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• Final Project



- Final Project
- EXAFS Theory

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- XAS Experiments

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Reading Assignment: Chapter 8.4

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Reading Assignment: Chapter 8.4

Homework Assignment #06: Chapter 6: 1,6,7,8,9 due Friday, November 15, 2024

- Final Project
- EXAFS Theory
- XAS Experiments
- Photoemission

Reading Assignment: Chapter 8.4

Homework Assignment #06: Chapter 6: 1,6,7,8,9 due Friday, November 15, 2024 Please send me your choices for General User proposal and final exam presentation. I need to approve them by the end of the week!

In-class student presentations on research topics

In-class student presentations on research topics

• Choose a research article which features a synchrotron technique



In-class student presentations on research topics

- Choose a research article which features a synchrotron technique
- Get it approved by instructor first!



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- Choose a research article which features a synchrotron technique
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- Schedule a 20 minute time on Final Exam Day (Thursday, May 4, 2023, 17:00-19:00)



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Final project - writing a General User Proposal



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Final project - writing a General User Proposal

• Think of a research problem (could be yours) that can be approached using synchrotron radiation techniques



In-class student presentations on research topics

- Choose a research article which features a synchrotron technique
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Final project - writing a General User Proposal

- Think of a research problem (could be yours) that can be approached using synchrotron radiation techniques
- Make proposal and get approval from instructor before starting

In-class student presentations on research topics

- Choose a research article which features a synchrotron technique
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Final project - writing a General User Proposal

- Think of a research problem (could be yours) that can be approached using synchrotron radiation techniques
- Make proposal and get approval from instructor before starting
- Must be different techique than your presentation!





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\mu(E)=\mu_0(E)+\Delta\mu(E)
$$

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\mu(E) = \mu_0(E) + \Delta \mu(E) = \mu_0(E)[1 + \chi(E)]
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\chi(k[E]) = \frac{\mu(E) - \mu_0(E)}{\mu_0(E)},
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\mu(E) \sim |\langle i|\mathcal{H}|f\rangle|^2
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 $\langle i|$  is the initial state which has a core level electron and the photon. This is not altered by the neighboring atom.



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 $|f\rangle$  is the final state which has a photoelectron, a hole in the core, and no photon. This is altered by the neighboring atom: the photoelectron scatters.





Writing  $|f\rangle = |f_0 + \Delta f\rangle$ , where  $\Delta f$  gives the change in photoelectron final state due to backscattering from the neighboring atom, we can expand  $\mu$  to get

 $\mu(E) \sim |\langle i|\mathcal{H}|f\rangle|^2$ 



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Compare this to  $\mu(E) = \mu_0(E)[1 + \chi(E)]$  and we see that



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 $\mu_0(E) \sim |\langle i | \mathcal{H} | f_0 \rangle|^2$ atomic background



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 $\mu_0(E) \sim |\langle i|\mathcal{H}|f_0\rangle|^2$  $\gamma(E) \sim \langle i | \mathcal{H} | \Delta f \rangle$ atomic background XAFS oscillations

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\chi(E) \sim \langle i|\mathcal{H}|\Delta f\rangle \sim \langle i|\Delta f\rangle \quad \text{XAFS oscillations}
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\chi(E) \sim \langle i|\Delta f\rangle \sim \int \psi_{\text{core}} \psi_{\text{scatt}}(r) \, dr
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\chi(E) \sim \langle i|\Delta f\rangle \sim \int \psi_{\text{core}} \psi_{\text{scatt}}(r) \, dr \sim \int \delta(r) \psi_{\text{scatt}}(r) \, dr = \psi_{\text{scatt}}(0)
$$

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Assume that emitted photoelectron is a spherical wave





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follow the electron as it:





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follow the electron as it:

a. leaves the absorbing atom



Assume that emitted photoelectron is a spherical wave

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follow the electron as it:

- a. leaves the absorbing atom
- b. scatters from the neighbor atom





Assume that emitted photoelectron is a spherical wave

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follow the electron as it:

- a. leaves the absorbing atom
- b. scatters from the neighbor atom
- c. returns to the absorbing atom

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\chi(k) \sim \psi_{scatt}(0) = \frac{e^{ikR}}{kR} [2kf(k)e^{i\delta(k)}]\frac{e^{ikR}}{kR}
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where scattering from the neighboring atom gives the amplitude  $f(k)$  and phase-shift  $\delta(k)$  to the photoelectron





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\chi(k) \sim \psi_{scatt}(0) = \frac{e^{ikR}}{kR} [2kf(k)e^{i\delta(k)}] \frac{e^{ikR}}{kR} = \frac{2e^{i(2kR + \delta(k))}}{kR^2} f(k)
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where scattering from the neighboring atom gives the amplitude  $f(k)$  and phase-shift  $\delta(k)$  to the photoelectron



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 $Z$  can usually be determined to  $\pm$ 5. Fe and O can be distinguished, but Fe and Mn cannot be





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Generally, the calculations (FEFF, etc) include these effects. We'll discuss of few of these in more detail  $\ldots$ 

Carlo Segre (Illinois Tech) **[PHYS 570 - Fall 2024](#page-0-0)** November 11, 2024 8 / 25

The photoelectron mean-free path



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for  $3 \AA^{-1} < k < 15 \AA^{-1}$ ,  $\lambda$  < 30 Å

along with the  $R^{-2}$  term this makes EXAFS a local atomic probe

for XANES  $(k\,<\,3\,\text{\AA}^{-1})$ , both  $\lambda$ and  $R^{-2}$  become large: making XANES not really a local probe





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This, and other experimental and theoretical issues, make EXAFS amplitudes (and therefore N) less precise than EXAFS phases (and therefore  $R$ )



The full EXAFS equation can be used to model and interpret experimental data



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Because we can compute  $f(k)$  and  $\delta(k)$ , and  $\lambda(k)$  we can determine Z, R, N, and  $\sigma^2$  for scattering paths to neighboring atoms by fitting the data.



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**Focussed Multiple Scattering Paths**





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For multi-bounce paths, the total amplitude depends on the angles in the photoelectron path

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For multi-bounce paths, the total amplitude depends on the angles in the photoelectron path Triangle Paths with angles  $45^{\circ} < \theta < 135^{\circ}$  aren't strong, but

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FEFF calculates these effects and includes them in  $f(k)$  and  $\delta(k)$  for the EXAFS equation so that all paths look the same in the analysis

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For first shell analysis, multiple scattering is hardly ever needed

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Carlo Segre (Illinois Tech) **[PHYS 570 - Fall 2024](#page-0-0)** November 11, 2024 14/25

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 $Sn_4P_3$ /graphite composite shows stable, reversible capacity of 610 mAh/g for 100 cycles at  $C/2$  compared to rapidly fading pure  $Sn_4P_3$  material.

# In situ EXAFS of  $Sn_4P_3$ /graphite





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Carlo Segre (Illinois Tech) [PHYS 570 - Fall 2024](#page-0-0) November 11, 2024 15 / 25

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# In situ EXAFS of  $Sn_4P_3$ /graphite





Results for in situ coin cell are close to the capacity of the unmodified cell at  $C/4$ , indicating good reversibility by the  $3^{rd}$  cycle.



By the third lithiation and third delithiation, the difference between pure  $\mathsf{Sn_4P_3}$  and the  $Sn_4P_3$ /graphite composite is clear.

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Carlo Segre (Illinois Tech) **[PHYS 570 - Fall 2024](#page-0-0)** November 11, 2024 16 / 25



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Carlo Segre (Illinois Tech) **[PHYS 570 - Fall 2024](#page-0-0)** November 11, 2024 16 / 25







Even at the 100<sup>th</sup> delithiation, the Sn<sub>4</sub>P<sub>3</sub>/graphite composite measured *ex situ* is showing the same features as at the  $3^{rd}$  cycle.



OCV spectrum fits well to  $\mathsf{Sn_4P_3}$  structure with an additional Sn-O path

 $\mathsf{Sn_4P_3}$  structure persists through first two cycles with possible enhancement of the Sn-Sn path at  $2.6 \text{ Å}$ 



On third lithiation (charge) the Sn-P path is gone and only Sn-Li remains Delithiation (discharge) produces Sn-P and Sn-Sn paths which are not those of  $Sn_{4}P_{3}$  but are reversible

# Example fits

Fit EXAFS for bond lengths and coordination numbers



The Sn-O peak at OCV is due to ball milling, which introduces oxygen.



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Carlo Segre (Illinois Tech) **[PHYS 570 - Fall 2024](#page-0-0)** November 11, 2024 19 / 25

# Example fits

#### Fit EXAFS for bond lengths and coordination numbers



By the 3<sup>rd</sup> lithiated state, the EXAFS is dominated by Sn-Li paths at 2.7  $Å$  and  $3.0 Å$ .



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# Example fits





At the 3<sup>rd</sup> delithiation, the Sn-P path reappears but at a shorter distance, in an amorphous  $SnP<sub>x</sub>$  phase.







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Sn-Sn distance close to those of metallic Sn indicate the presence of small Sn clusters which may never fully lithiate

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Sn-O distances remain constant, likely indicative of surface contamination

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Sn-O neighbors decrease quickly, remaining small and partially reversible up to 100 cycles

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The  $\sim$ 3.3 Sn-P neighbors in the delithiated state indicate a possibly tetrahedral Sn coordination in  $SnP<sub>x</sub>$ 

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Amorphous  $\text{SnP}_{x}$  fully formed at start of 3<sup>rd</sup> cycle



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Carlo Segre (Illinois Tech) [PHYS 570 - Fall 2024](#page-0-0) November 11, 2024 22 / 25



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a. Sn lithiating



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- a. Sn lithiating
- b.  $SnP<sub>x</sub>$  all gone





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- a. Sn lithiating
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- c. full lithiation



Amorphous  $\text{SnP}_{x}$  fully formed at start of 3<sup>rd</sup> cycle



- a. Sn lithiating
- b.  $SnP<sub>x</sub>$  all gone
- c. full lithiation
- d. Sn appears



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- a. Sn lithiating
- b.  $SnP<sub>x</sub>$  all gone
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- d. Sn appears
- e.  $SnP<sub>x</sub>$  appears





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- a. Sn lithiating
- b.  $SnP<sub>x</sub>$  all gone
- c. full lithiation
- d. Sn appears
- e.  $SnP<sub>x</sub>$  appears
	- f. Sn delithiated




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The dispersion relation of electrons in a solid,  $\mathcal{E}(\vec{q})$ can be probed by angle resolved photoemission since both the kinetic energy,  $\mathcal{E}_{kin}$ , and the angle,  $\theta$  are measured





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The work function,  $\phi$ , is the minimum energy required to promote an electron from the top of the valence band at the Fermi energy,  $\mathcal{E}_F$ , to the vacuum energy,  $\mathcal{E}_{V}$ 





With the incident photon energy,  $\hbar\omega$ , held constant, an analyzer is used to measure the kinetic energy,  $\mathcal{E}_{kin}$ , of the photoelectrons emitted from the surface of the sample

Carlo Segre (Illinois Tech) **[PHYS 570 - Fall 2024](#page-0-0)** November 11, 2024 24 / 25





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the core states are used to fingerprint the chemical composition of the sample

The electric field between the two hemispheres of radius  $R_1$  and  $R_2$  has a  $R^2$  dependence from the center of the hemispheres



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Electrons with different azimuthal exit angles  $\omega$  will map to different positions on the 2D detector

