

Today's Outline - February 20, 2020

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- HW #02 solutions

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Homework Assignment #03:

Chapter 3:1,3,4,6,8

due Thursday, February 27, 2020

HW #02

1. Knowing that the photoelectric absorption of an element scales as the inverse of the energy cubed, calculate:
 - (a) the absorption coefficient at 10keV for copper when the value at 5keV is 1698.3 cm^{-1} ;
 - (b) The actual absorption coefficient of copper at 10keV is 1942.1 cm^{-1} , why is this so different than your calculated value?
2. A 30 cm long, ionization chamber, filled with 80% helium and 20% nitrogen gases at 1 atmosphere, is being used to measure the photon rate (photons/sec) in a synchrotron beamline at 12 keV. If a current of 10 nA is measured, what is the photon flux entering the ionization chamber?
3. A 5 cm deep ionization chamber is used to measure the fluorescence from a sample containing arsenic (As). Using any noble gases or nitrogen, determine a gas fill (at 1 atmosphere) for this chamber which absorbs at least 60% of the incident photons. How does this change if you are measuring the fluorescence from ruthenium (Ru)?

HW #02

4. Calculate the critical angle of reflection of 10 keV and 30 keV x-rays for:

- (a) A slab of glass (SiO_2);
- (b) A thick chromium mirror;
- (c) A thick platinum mirror.
- (d) If the incident x-ray beam is 2 mm high, what length of mirror is required to reflect the entire beam for each material?

5. Calculate the fraction of silver (Ag) fluorescence x-rays which are absorbed in a 1 mm thick silicon (Si) detector and the charge pulse expected for each absorbed photon. Repeat the calculation for a 1 mm thick germanium (Ge) detector.

SAXS review

The SAXS scattered intensity from a dilute solution depends on the single particle form factor, $\mathcal{F}(\vec{Q})$, the volume of the particle, V_p , and the density difference from the solvent, $\Delta\rho = (\rho_{sl,p} - \rho_{sl,0})$

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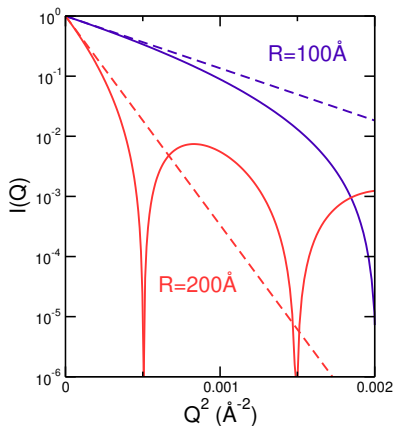
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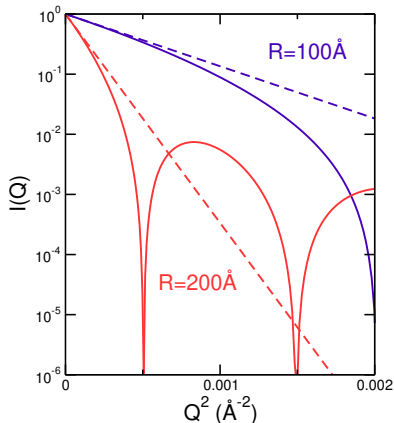
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$$R_g^2 = \frac{\int_{V_p} \rho_{sl,p}(\vec{r}) r^2 dV_p}{\int_{V_p} \rho_{sl,p}(\vec{r}) dV_p}$$

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$$I(q) = B_{bkg} + \sum_{i=1}^N G_i e^{-\frac{q^2 R_{g,i}^2}{3}} + e^{-\frac{q^2 R_{g,i-1}^2}{3}} B_i \left[\frac{\left(\operatorname{erf} \left\{ \frac{q R_{g,i}}{\sqrt{6}} \right\} \right)^3}{q} \right]^{P_i}$$

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The sum is over structural levels starting with the smallest. For each level there is a Guinier exponential prefactor (G_i), a radius of gyration ($R_{g,i}$), a power law constant prefactor (B_i), and a power law exponent (P_i).

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It is important not to include more levels than are significant physically

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- Nucleation and growth of & glycine crystals

SAXS of irradiated Zn nanoparticles

Zn nanoparticles formed in SiO₂ by ion implantation are irradiated with high energy Xe⁺¹⁴ ions.

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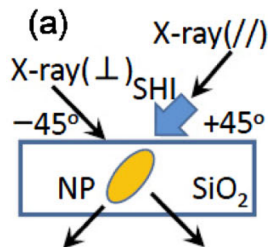
SAXS is measured using 18 keV x-rays both parallel and perpendicular to the direction of Xe⁺¹⁴ irradiation.

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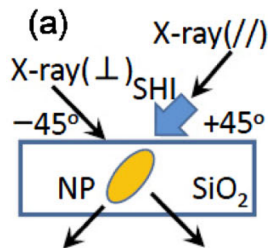
Expt. geometry

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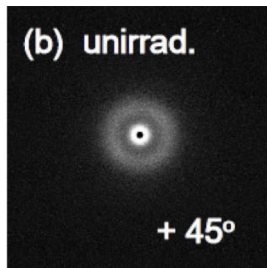
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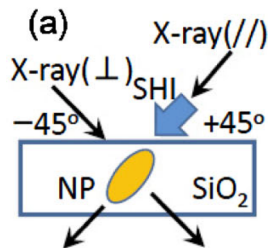
Unirradiated

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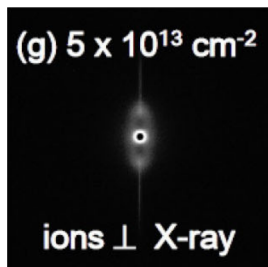
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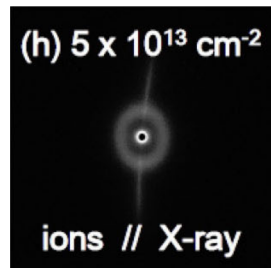
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Irradiated ⊥ x-rays



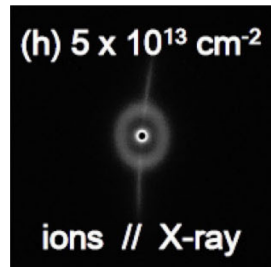
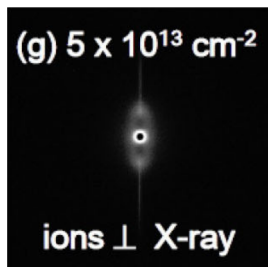
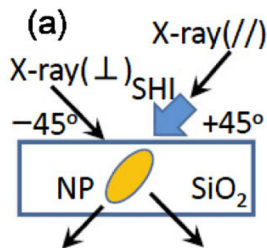
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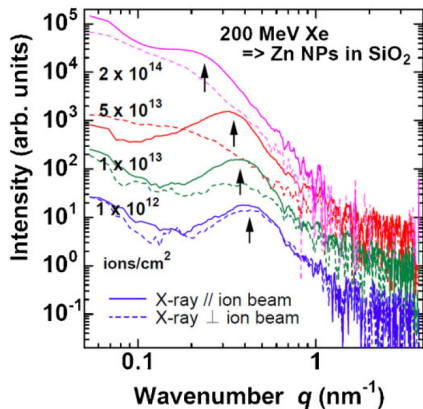
Irradiated \perp x-rays

Irradiated \parallel x-rays

Straight lines are due to ion tracks, seen in both directions and which persist to the highest fluences.

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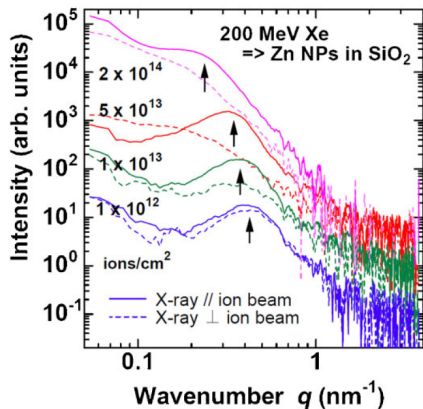
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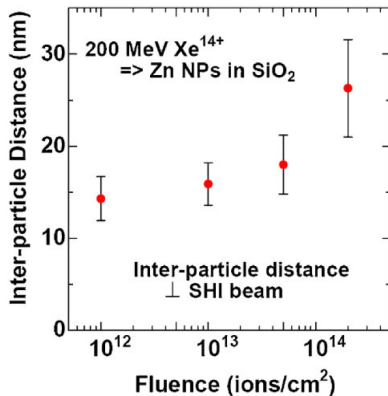
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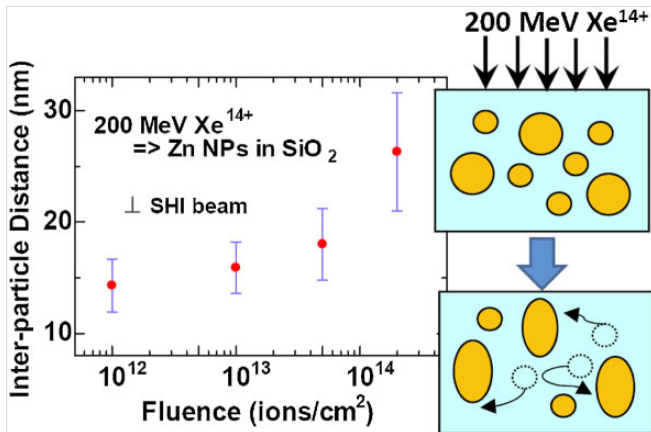
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Interparticle distance increases as a function of irradiation fluence

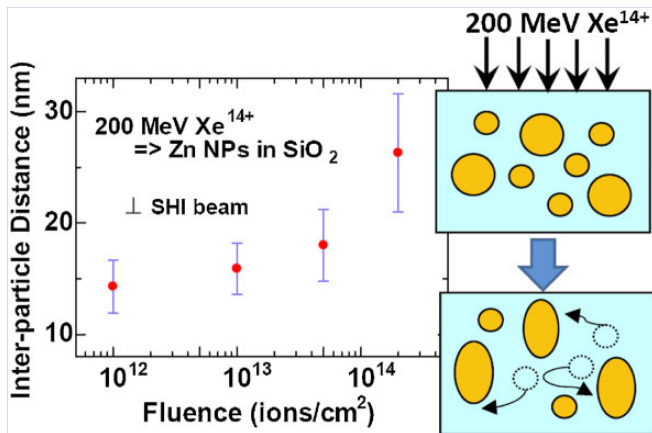
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Growth of interparticle spacing is due to dissolution and re-agglomeration with fluence leading to larger interparticle spacings

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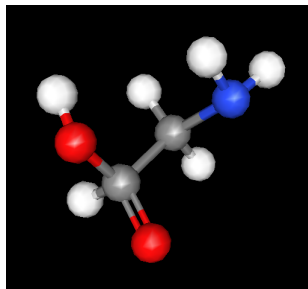
Nucleation & growth of glycine

Can SAXS help us understand the nucleation and growth of a simple molecule which is the prototype for pharmaceutical compounds?

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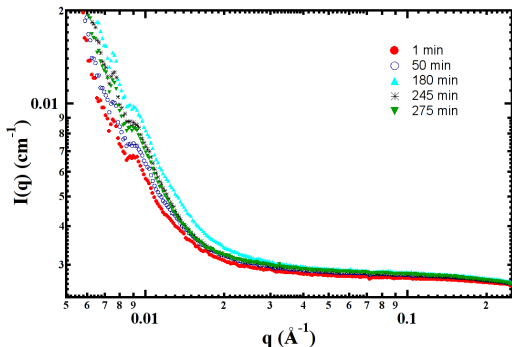
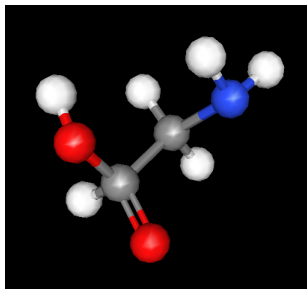
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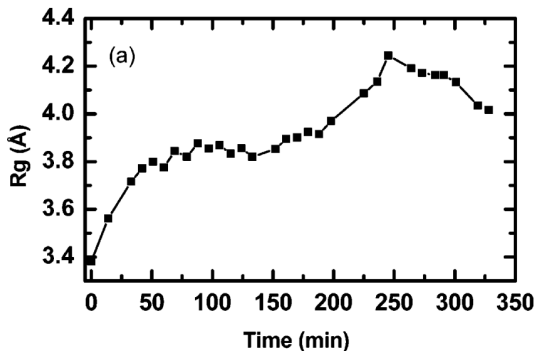
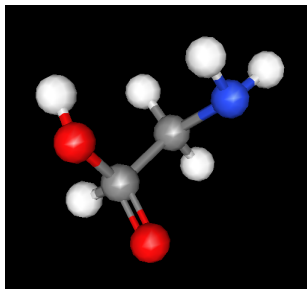


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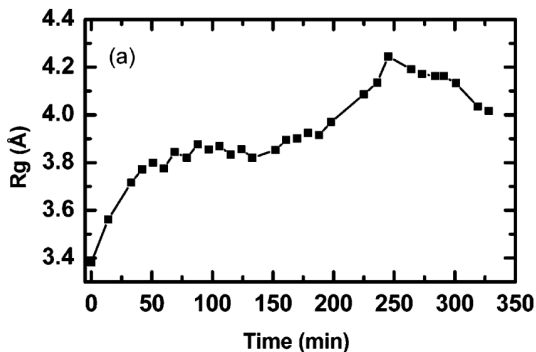
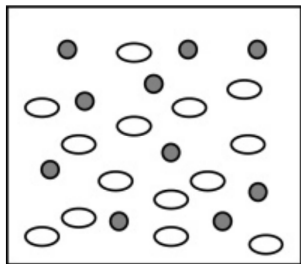


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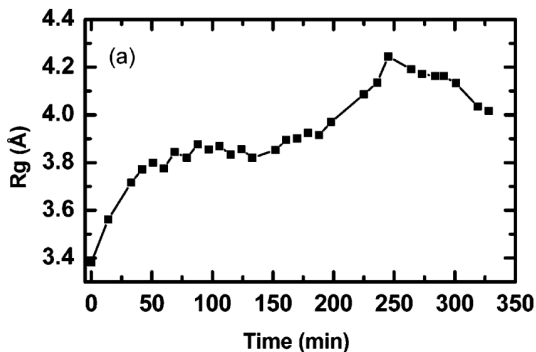
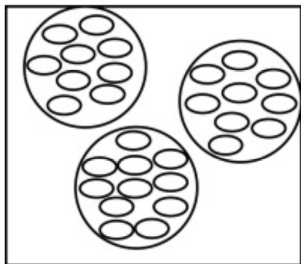


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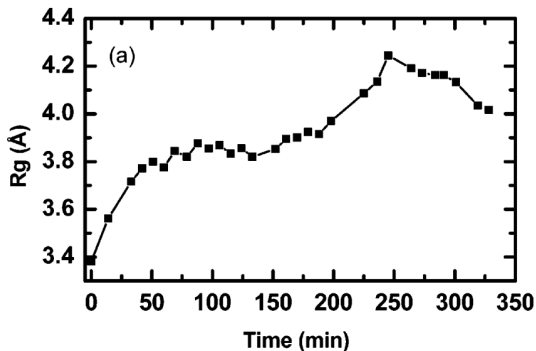
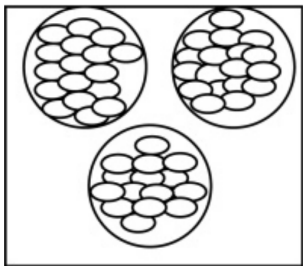


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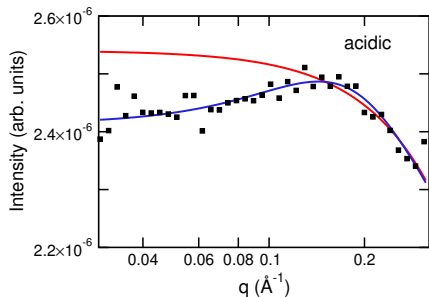
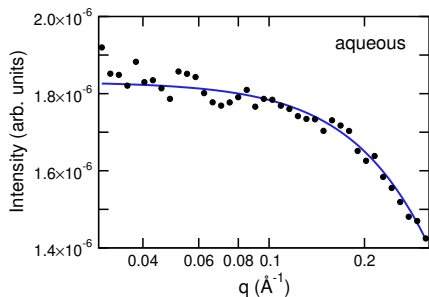
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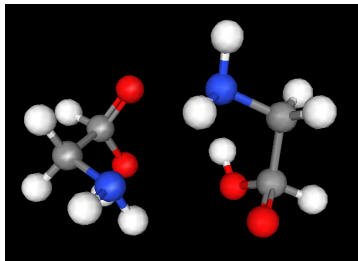
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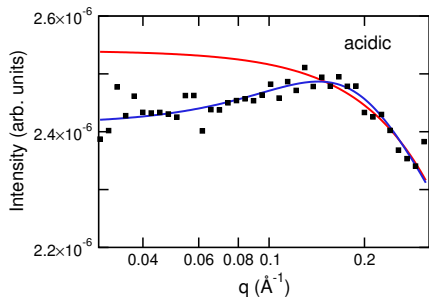
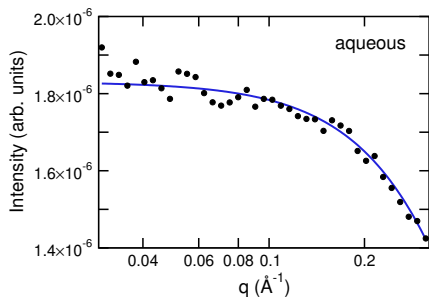
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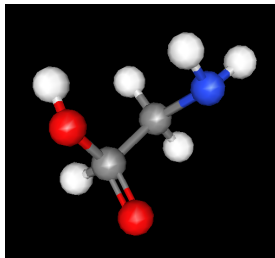
Glycine nucleation



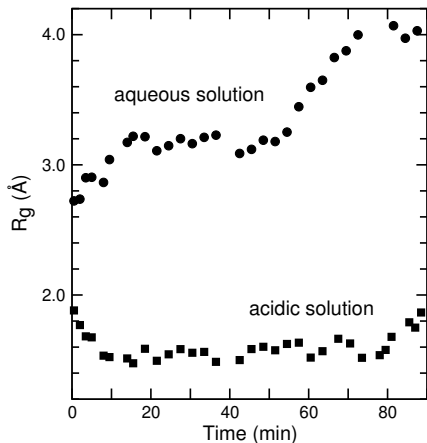
Long nucleation times due to heating from absorbed 12 keV x-rays.

Change to 25 keV x-rays reduces crystallization time to under 90 min

Different polymorphs are produced under varying conditions so study extended to both neutral and acidic solutions



Glycine R_g



in aqueous solution, R_g implies dimerization and increases due to aggregation until crystallization

in acidic solution, R_g remains small and implies that no dimerization or aggregation occurs before nucleation

"Relationship between self-association of glycine molecules in supersaturated solution and solid state outcome",
D. Erdemir et al. *Phys. Rev. Lett.* **99**, 115702 (2007)

Size exclusion chromatography SAXS

SAXS of biological molecules is an excellent way of getting some information about the molecules as they exist in solution.

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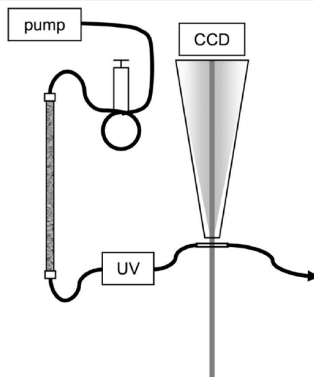
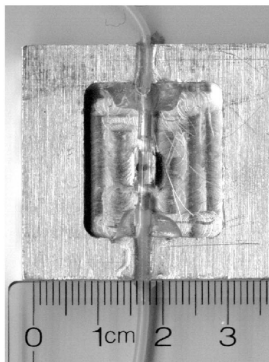
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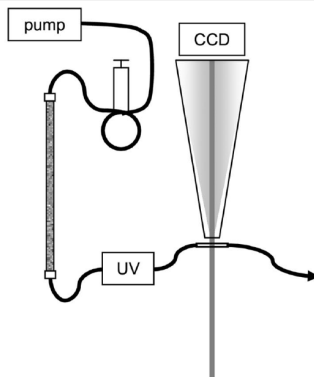
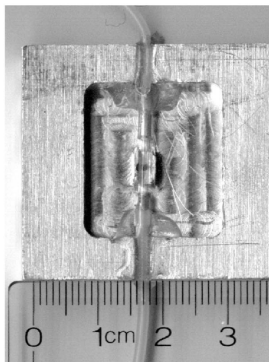
Mathew, Mirza & Menhart, "Liquid-chromatography-coupled SAXS for accurate sizing of aggregating proteins," *J. Synchrotron Rad.* **11**, 314-318 (2004) developed a technique which is now being used routinely in biological SAXS, called Size Exclusion Chromatography SAXS.

Size exclusion chromatography SAXS



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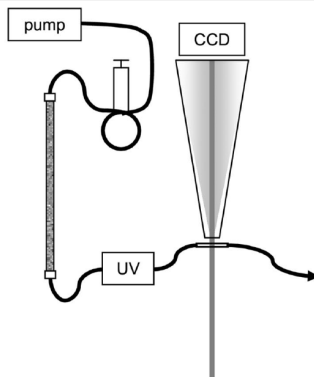
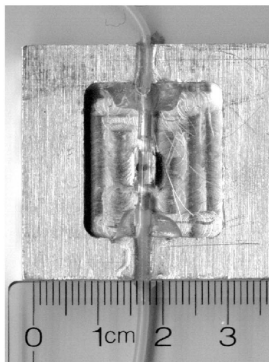
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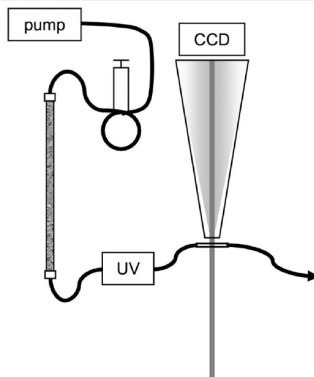
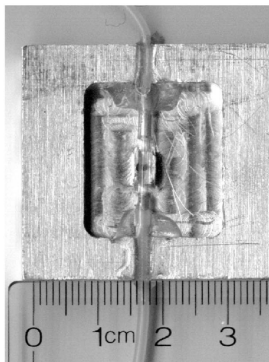
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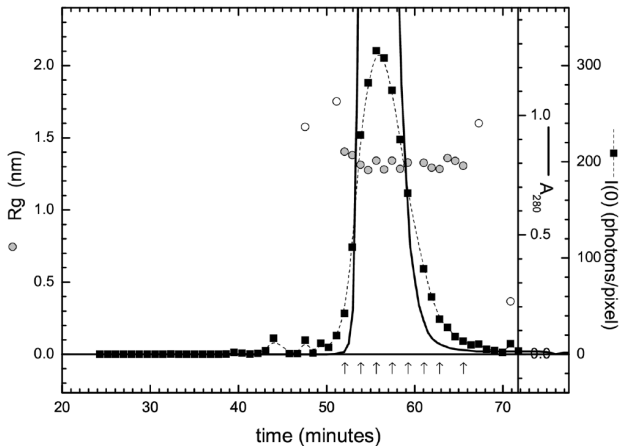
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samples of (1) cytochrome c, (2) plasminogen, (3) mixture of cytochrome c bovine serum albumin, and blue dextran

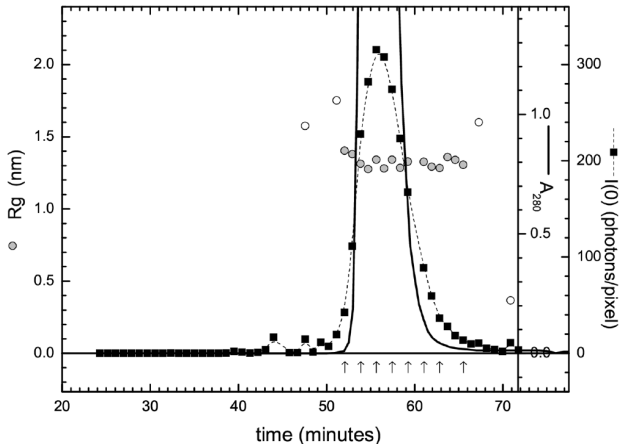
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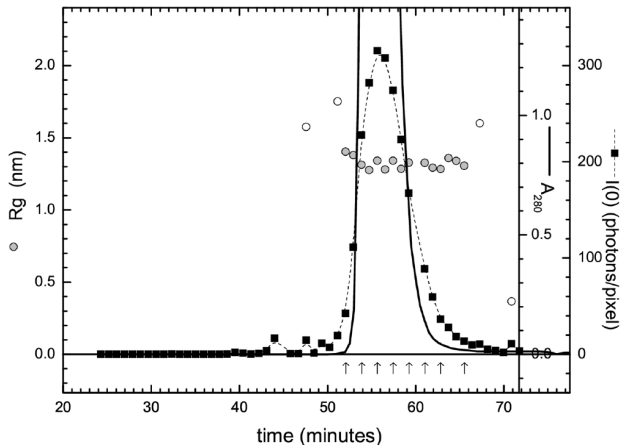
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Forward scatter (black squares) gives a measure of the total number of electrons in the beam

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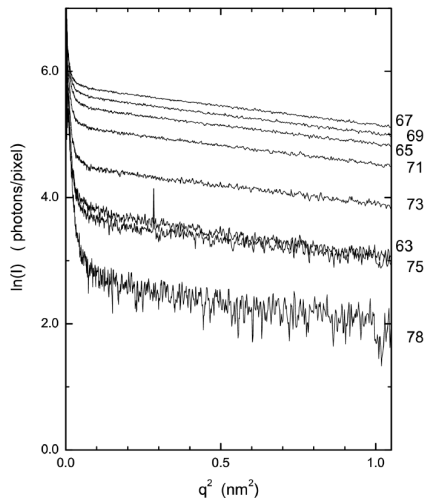
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Forward scatter (black squares) gives a measure of the total number of electrons in the beam R_g is constant throughout the main peak.

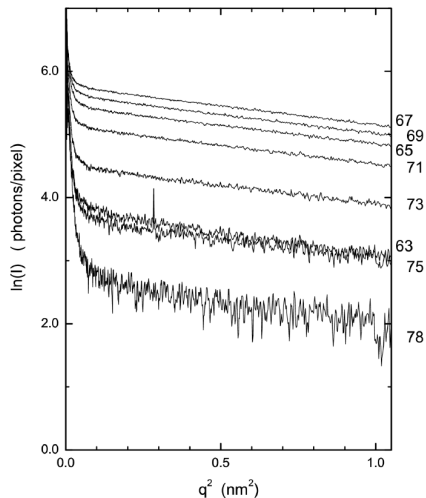
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Cytochrome c - Guinier plots



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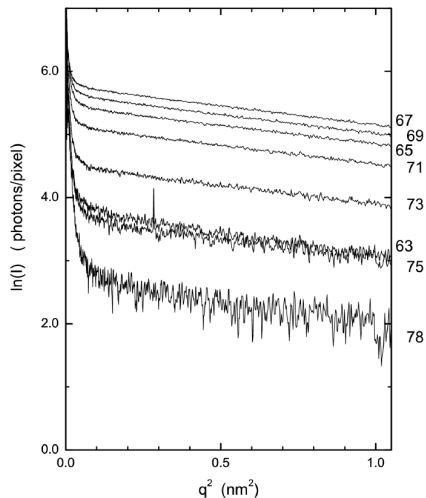
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Plot from times marked with arrows on R_g plot.

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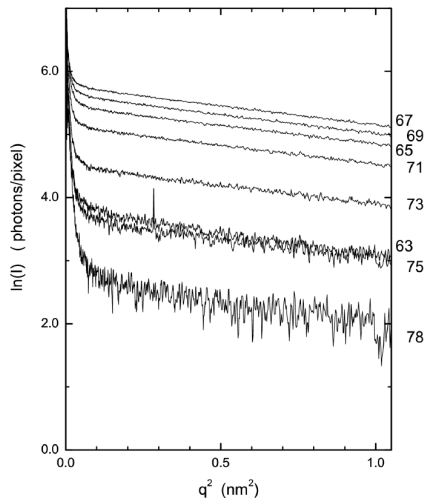


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Guinier plots are parallel, indicating a single species present (a single critical exponent).

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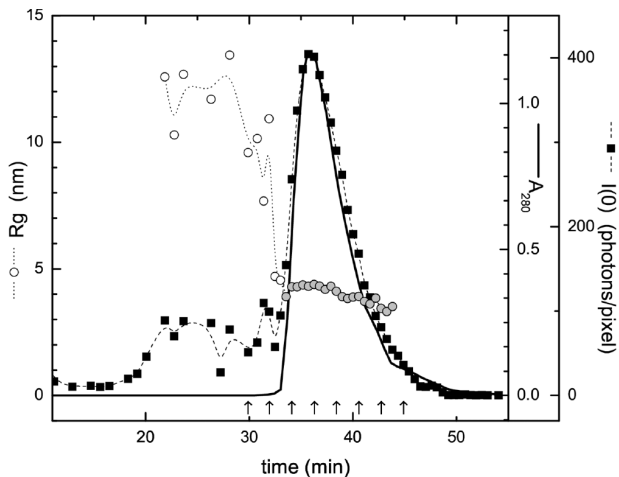
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Even lowest intensity data set gives a consistent R_g .

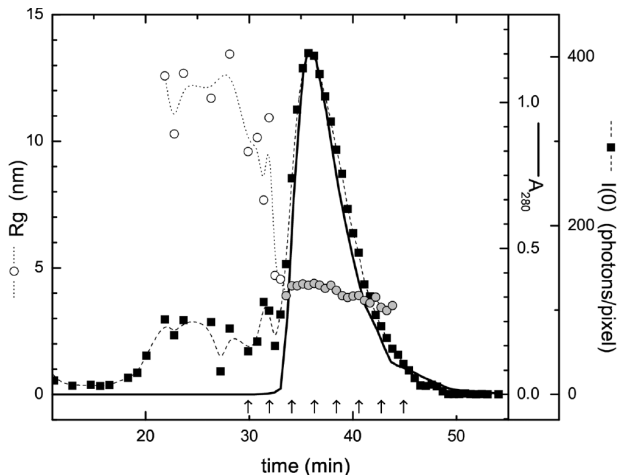
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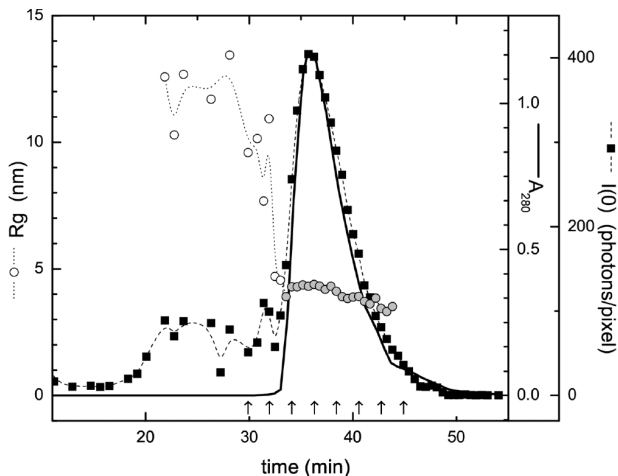
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Constant R_g in region where $A_{UV}/I(0)$ is constant.

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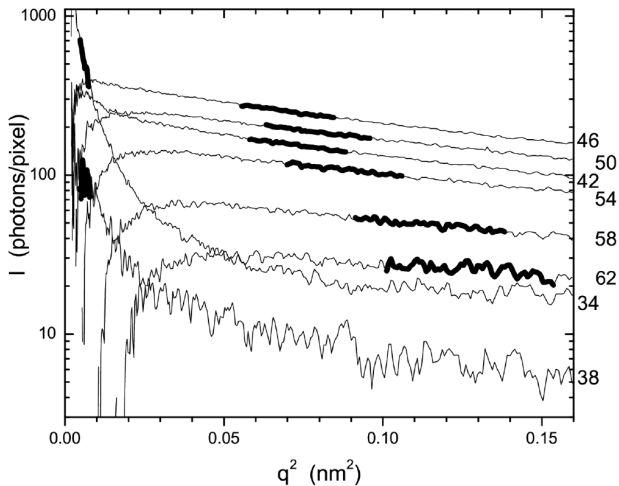
Plasminogen



Constant R_g in region where $A_{UV}/I(0)$ is constant. Aggregates precede the main peak and show wildly varying R_g .

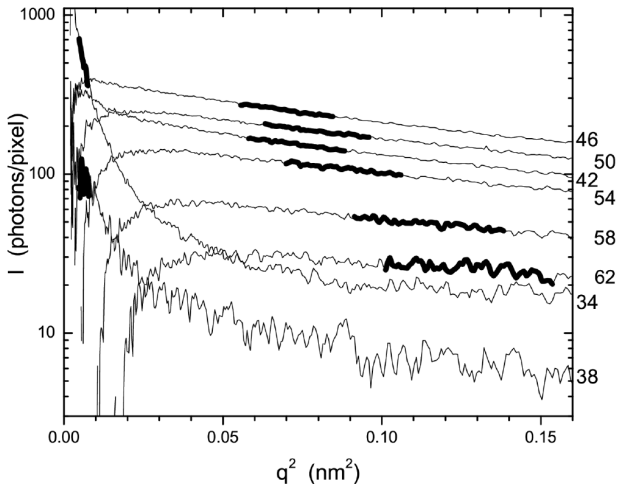
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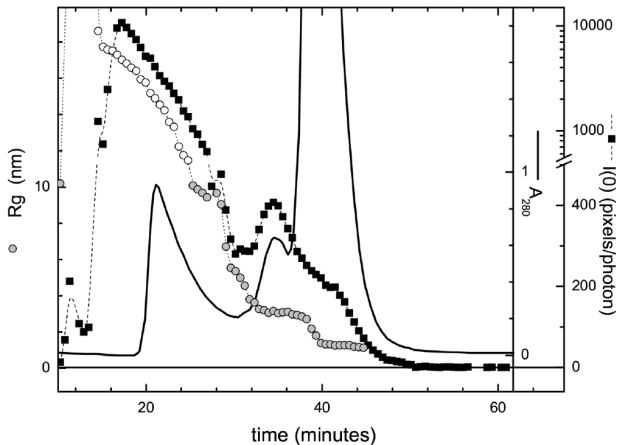
Plasminogen - Guinier plots



Guinier plots labeled 34 and 38 show presence of aggregates and the slopes are not parallel, indicating multiple sized species

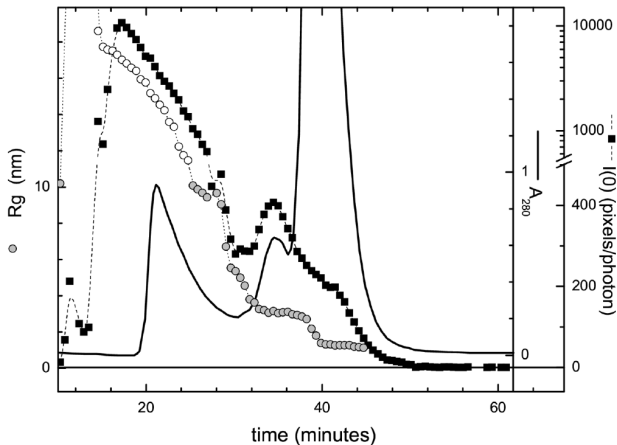
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Three component mixture



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Three component mixture



Two of the three components show consistent R_g and can be individually identified despite the overlap.

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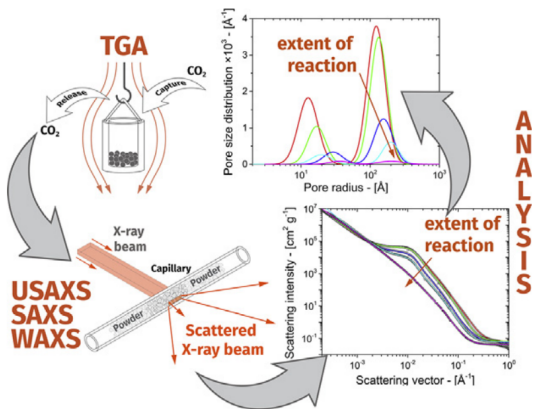
Porosity in CaO calcination

SAXS was used to study the nature of the porosity and particle sizes of CaO obtained by calcining CaCO₃.

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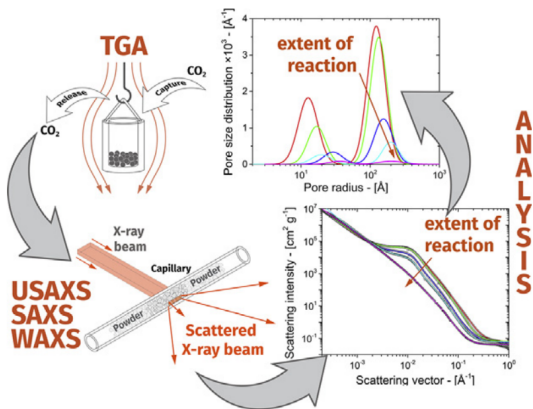


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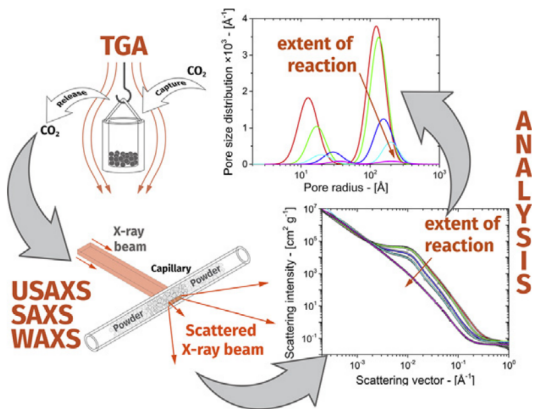
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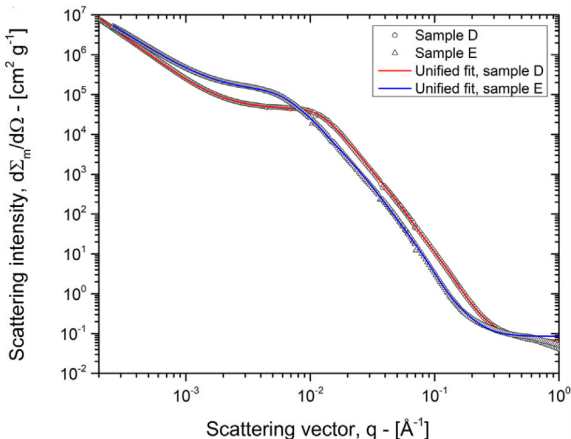
The samples were studied ex-situ at Sector 9-ID using USAXS and analyzed with a unified fit model

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Porosity in CaO calcination

Sample D was calcined at 900 °C for 50 minutes while sample E was calcined at the same temperature for 240 minutes

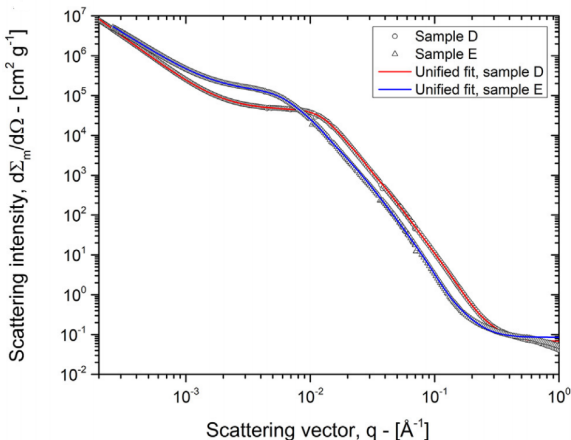


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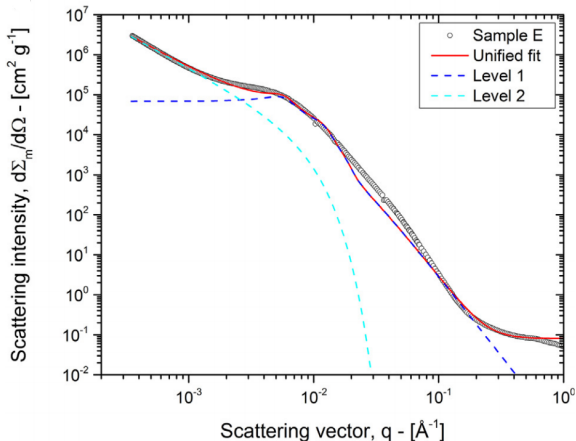
The SAXS shows the grain growth evolution between the two samples and it is clear that the samples need a multilevel unified fit



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The components of the unified fit model are shown for a two level fit and it is clear that 2 levels are insufficient.

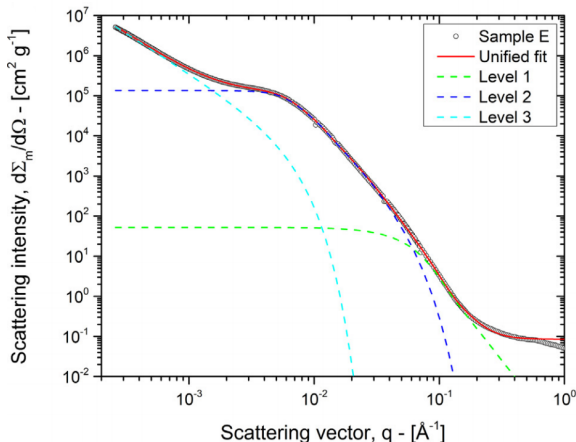


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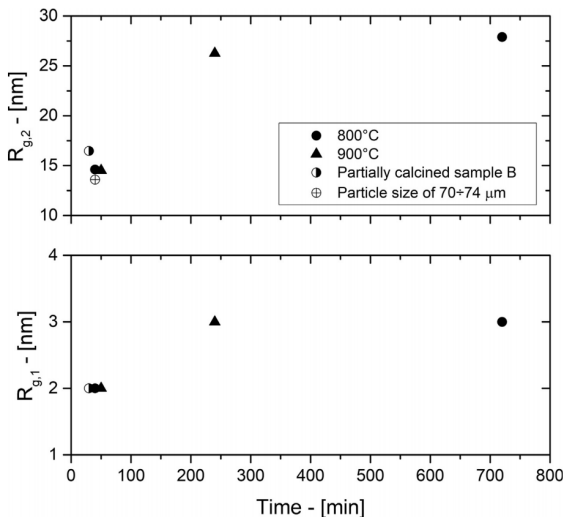
A three level fit works well for the calcined samples and from this one can extract the pore sized for two different pore populations in the calcined samples



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Porosity in CaO calcination

Fitting a series of samples calcined at varying temperatures and times shows the evolution of the radii of gyration of the two populations corresponding to the pore sizes

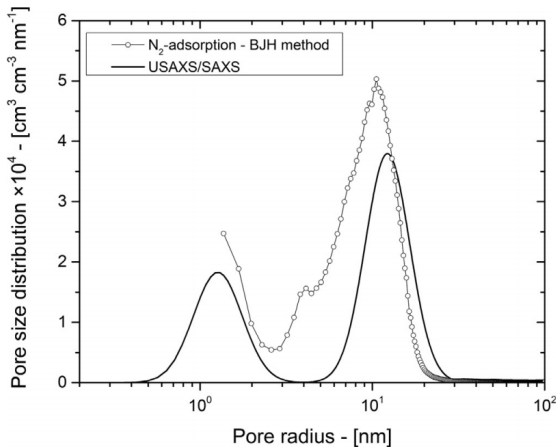


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