

# Today's outline - February 11, 2020

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Homework Assignment #02:  
Problems on Blackboard  
due Tuesday, February 18, 2020

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- Fresnel lenses and zone plates
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Homework Assignment #02:  
Problems on Blackboard  
due Tuesday, February 18, 2020

APS Visit:  
10-BM: Friday, April 24, 2020

# Beamtime at MRCAT

One day has been set aside for our class to be at Sector 10 MRCAT at the Advanced Photon Source



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I will try to record the session for those of you not in Chicago

# Writing a General User Proposal

1. Log into the APS site
2. Start a general user proposal
3. Add an Abstract
4. Choose a beam line
5. Answer the 6 important questions

A tutorial can be found on the course home page

[http://csrri.iit.edu/~segre/phys570/20S/gu\\_proposal.html](http://csrri.iit.edu/~segre/phys570/20S/gu_proposal.html)

# Register & log into the APS Portal



## User Registration for Advanced Photon Source (APS) and Center for Nanoscale Materials (CNM)

Welcome Users and Visitors

### New Users

- Never been assigned an Argonne ID badge number
- Never been to Argonne before
- Plan to conduct hands-on work
- Need remote computer access to an Argonne User Facility

New User

### Returning Users

- Update existing biographical/contact information
- Renew my approval for site access

Note: You must have a user badge # to access this site. Badge number appears on the back of your badge, see below.



My APS Portal

CNM Returning User

### Visiting Argonne

- Not conducting hands-on work/research
- Short-term visit to Argonne (e.g. a meeting speaker, family member, traveling companion, conference/workshop attendee, tour group member)
- Only utilizing the ANL/APS guest computer network
- Not a current facility user

Visitor Pass

Need assistance? E-Mail: [apsuser@aps.anl.gov](mailto:apsuser@aps.anl.gov).

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# APS Portal details



Advanced Photon Source  
» an Office of Science User Facility



My APS Portal

Welcome: Carlo U. Segre [Get Help](#) [Logout](#)

[Home](#) [My Check-in](#) [User Agreement](#) [My Training](#) [My Proposals](#) [My ESAFs](#) [My EEFs](#) [My Registration](#)

[Take me to APS Beam Time Request System](#)

gup ID	Spokesperson	Submit Date	Proposal Title	Status
<a href="#">58123</a>	Yiqing Zhang	01/31/2018	Ex-situ XAS study of Ni,Co,Fe modified po...	SUBMITT...
<a href="#">58111</a>	Kamil Kucuk	01/29/2018	In-situ XAS study of Li2FeSiO4 sample as...	SUBMITT...
<a href="#">57789</a>	Carlo Segre	11/15/2017	EXAFS of metal oxide materials	SUBMITT...
<a href="#">57415</a>	Andrew Breshears	10/27/2017	Study of metal coordination environment o...	ACTIVE
<a href="#">56390</a>	Elena Timofeeva	10/04/2017	Investigation of x-ray beam energy on radi...	SUBMITT...
<a href="#">56128</a>	Yujia Ding	08/31/2017	In situ EXAFS study of SnS2-based graph...	SUBMITT...
<a href="#">55959</a>	Shankar Aryal	07/29/2017	Ex situ XAS measurement of NMC cathod...	SUBMITT...
<a href="#">55146</a>	Christopher Murray	07/07/2017	Operando Characterization of Bimetallic N...	ACTIVE
<a href="#">54740</a>	Leon Shaw	07/02/2017	Analysis of Novel Electrode Materials for ...	ACTIVE
<a href="#">54572</a>	Carlo Segre	06/07/2017	Illinois Tech ex-situ battery EXAFS	SUBMITT...
<a href="#">54571</a>	Shankar Aryal		In situ XAS study of Li rich composite oxid...	NEW

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# Start a General User Proposal



## Type of Beam Time Request - Main Menu

Logout

Welcome to the APS Beam Time Access System.

Please select an action:

### Create a New Proposal

General Users

Partner Users

CAT Members

CAT Beamline Staff

Facility Beamline Staff

APS  CNM

### Existing Proposals

Find Proposal:

Proposal #

numeric portion only

Submit Query

Find Proposal by Request Type:

General User

Submit Query

Request Time for Proposal:

Proposal #

numeric portion only

Submit Query

[Advanced Search »](#)

### Administration

Beamlines Admin

Schedule Admin

# Add title & answer details



GUP-1

General User Program: gu\_program@aps.anl.gov, 630-252-9090

Technical assistance: mis\_mgrs@aps.anl.gov

\*Proposal  
Title:

Shifts Recommended by PRP:	Shifts Allocated by BAC or Scheduled by Beamline in current cycle	Shifts Used to date:	Shifts Remaining:	
not available	(0)	(0)		not available

Do you want this proposal to be considered for project status? <a href="#">description</a>	Yes <input type="radio"/>	No <input checked="" type="radio"/>
Does this proposal require <a href="#">mail-in service</a> ?	Yes <input type="radio"/>	No <input checked="" type="radio"/>
*Does this research involve macromolecular crystallography (single crystals) ?	Yes <input type="radio"/>	No <input type="radio"/>
*Will the data collected be considered proprietary ?	Yes <input type="radio"/>	No <input type="radio"/>
*Will the data collected be considered classified ?	Yes <input type="radio"/>	No <input type="radio"/>
Does this research involve human subjects or materials ?	Yes <input type="radio"/>	No <input type="radio"/>
Does this research involve live animals?	Yes <input type="radio"/>	No <input type="radio"/>
*Are there known safety hazards associated with the proposed experimental procedures or your samples ?	Yes <input type="radio"/>	No <input type="radio"/>
*Does this research involve the use of radioactive samples/materials ?	Yes <input type="radio"/>	No <input type="radio"/>
*Does this research involve samples/materials that require a BSL 2 or BSL 3 facility?	Yes <input type="radio"/>	No <input type="radio"/>
Is this research required for a student's thesis ?	Yes <input type="radio"/>	No <input type="radio"/>
Have you spoken to a beamline staff member?	Yes <input type="radio"/>	No <input type="radio"/>
Does this proposal involve the use of a sample from the ATR library?	Yes <input type="radio"/>	No <input type="radio"/>
*Is this proposal related to another general user proposal ? If so, which one(s) and how ?	Yes <input type="radio"/>	No <input type="radio"/>

# More details

(500 characters or less)

**\*Subject of Research:**

- |  |   |   |
|--|---|---|
| <input type="checkbox"/> Materials science | <input type="checkbox"/> Physics                                    | <input type="checkbox"/> Chemistry                                  |
| <input type="checkbox"/> Polymers          | <input type="checkbox"/> Medical applications                       | <input type="checkbox"/> Biological and life sciences               |
| <input type="checkbox"/> Earth sciences    | <input type="checkbox"/> Environmental sciences                     | <input type="checkbox"/> Optics (excluding x-ray optics)            |
| <input type="checkbox"/> Engineering       | <input type="checkbox"/> Instrumentation related to user facilities | <input type="checkbox"/> Purchase of specialty service or materials |
| <input type="checkbox"/> Other (specify)   | <b>Specify Other :</b> <input type="text"/>                         |   |

Next

Pressing SAVE will allow you to save this proposal and continue to make changes. Notifications will not be sent.

Save

Pressing SUBMIT will save this proposal AND notifications will be sent to the APS. No changes can be made thereafter.

Submit

GUP-1

ANL

# Select experimenters



## APS - General User Proposal

Main Menu Search Criteria Instructions Logout

General **Experimenters** Abstract Beamtime Request Questions Review Panel

GUP 30230

General User Program: gu\_programs@aps.anl.gov, 630 252 9090

Technical assistance: mis\_mgrs@aps.anl.gov

Spokesperson: [Find](#)

First Name :

Last Name

\*Phone:

\*Email

\*Badge

Institution:

Mailing Address:

Experimenters  
Coming to APS:

	Badge	First Name	Last Name	Affiliation	Phone	Email	Delete
<a href="#">Find</a>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
<a href="#">Find</a>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
<a href="#">Find</a>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
<a href="#">Find</a>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>

Experimenters  
Not Coming to APS:

	Badge	First Name	Last Name	Affiliation	Phone	Email	Delete
<a href="#">Find</a>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
<a href="#">Find</a>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
<a href="#">Find</a>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
<a href="#">Find</a>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>

[Back](#)

[Generate Report](#)

[Next](#)

# Insert abstract



## APS - General User Proposal

Main Menu Search Criteria Instructions Logout

General Experimenters **Abstract** Beamtime Request Questions Review Panel

GUP-30230

General User Program: gu\_program@aps.anl.gov, 630 252 9090

Technical assistance: mis\_mgrs@aps.anl.gov

You may attach supporting PDF documents to this proposal. [Click here to attach/detach files](#)

List of Attachments **Abstract of Proposed Research**

**NOTES :**

- You **MUST** have an abstract below. Attaching only a PDF is not enough.
- Abstract **MUST** be less than 4000 characters including spaces.
- The abstract and proposal title may become public information.
- Don't enter any carriage return.
- The proposal system runs on the WEISO8859P1 (Western European, Latin) character set. Characters you enter into the system that are Unicode or otherwise not a subset of WEISO8859P1 will not render properly in the report of your proposal. Typically these are greek, super/subscript characters, etc. Click here to see a list of [valid characters and Proposal Content and Style Guidelines](#)

Characters Remaining :

# Make Beam Time Request



APS - General User Proposal

Main Menu Search Criteria Instructions Logout

General Experimenters Abstract **Beamtime Request** Questions Review Panel

GUP 30230

General User Program: gu\_program@aps.anl.gov, 630.252.9090

Technical assistance: mis\_mgrs@aps.anl.gov

<a href="#">Rapid Access Description</a>	<a href="#">Make New Request</a>	<b>Total 8-hour shifts requested for the LIFE OF THE PROPOSAL</b>	<input type="text"/>
		<b>Total 8-hour shifts recommended by the Proposal Review Panel for the LIFE OF THE PROPOSAL :</b>	not available
		<b>Total shifts used and scheduled (or allocated) to date:</b>	0
		<b>Number of the shifts remaining</b>	not available
		<b>*For which scheduling period are you applying?</b>	<input type="text"/> Status :
		<b>Techniques Required:</b>	<input type="text"/> <input type="text"/> <input type="text"/>
		<b>*Choice Of Beamline:</b> (The drop-down list will show when you click on one of scheduling periods, each beamline choice should be different.)	Select One Beamline <input type="text"/> 1st Select One Beamline <input type="text"/> 2nd Select One Beamline <input type="text"/> 3rd
		<b>*Please select the instrument based on your beamline selection:</b> (Click on beamline drop-down above to display the instrument drop-down if existing.)	<input type="text"/> For 1st beamline <input type="text"/> For 2nd beamline <input type="text"/> For 3rd beamline
		<b>Any appropriate beamline</b>	<input checked="" type="checkbox"/>
		<b>*Number of 8-hour shifts requested for THIS scheduling period</b>	<input type="text"/>
		<b>Minimum number of usable shifts per visit:</b>	<input type="text"/>

# Beam Time Request continued

<b>Do you have specific scheduling requirements ?</b>																
<b>What equipment is required ? What equipment will you bring ?</b>																
<b>Please list any new publications resulting from your work at the APS.</b>																
<b>Describe the progress made during your most recent beamtime. (2000 characters including spaces)</b>																
<b>Prefered Dates (MM/DD/YYYY)</b>	<table><thead><tr><th data-bbox="852 570 989 586">From</th><th data-bbox="989 570 1016 586">to</th><th data-bbox="1016 570 1167 586">To</th></tr></thead><tbody><tr><td><input type="text"/></td><td></td><td><input type="text"/></td></tr><tr><td><input type="text"/></td><td></td><td><input type="text"/></td></tr><tr><td><input type="text"/></td><td></td><td><input type="text"/></td></tr><tr><td><input type="text"/></td><td></td><td><input type="text"/></td></tr></tbody></table>	From	to	To	<input type="text"/>		<input type="text"/>	<input type="text"/>		<input type="text"/>	<input type="text"/>		<input type="text"/>	<input type="text"/>		<input type="text"/>
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<b>Unacceptable Dates (MM/DD/YYYY)</b>	<table><thead><tr><th data-bbox="852 721 989 736">From</th><th data-bbox="989 721 1016 736">to</th><th data-bbox="1016 721 1167 736">To</th></tr></thead><tbody><tr><td><input type="text"/></td><td></td><td><input type="text"/></td></tr><tr><td><input type="text"/></td><td></td><td><input type="text"/></td></tr><tr><td><input type="text"/></td><td></td><td><input type="text"/></td></tr><tr><td><input type="text"/></td><td></td><td><input type="text"/></td></tr></tbody></table>	From	to	To	<input type="text"/>		<input type="text"/>	<input type="text"/>		<input type="text"/>	<input type="text"/>		<input type="text"/>	<input type="text"/>		<input type="text"/>
From	to	To														
<input type="text"/>		<input type="text"/>														
<input type="text"/>		<input type="text"/>														
<input type="text"/>		<input type="text"/>														
<input type="text"/>		<input type="text"/>														

# Answer the 6 important questions



GUP 30230

General User Program: gu\_program@aps.anl.gov, 630 252 9090

Technical assistance: mis\_mgrs@aps.anl.gov

### Please Note:

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### Please specify the funding source(s) for your proposed research:

- |   |   |   |
|---|---|---|
| <input type="checkbox"/> DOD (specify)                          | <input type="checkbox"/> DOE, Office of Basic Energy Sciences | <input type="checkbox"/> DOE, Office of Biological and Environmental Research |
| <input type="checkbox"/> DOE, Other (specify)                   | <input type="checkbox"/> Foreign (specify)                    | <input type="checkbox"/> HHIH   |
| <input type="checkbox"/> Howard Hughes Medical Institute (HHMI) | <input type="checkbox"/> Industry                             | <input type="checkbox"/> NASA   |
| <input type="checkbox"/> NIH                                    | <input type="checkbox"/> NSF                                  | <input type="checkbox"/> Other U.S. Government                                |
| <input type="checkbox"/> USDA                                   | <input type="checkbox"/> Other (specify)                      | <b>Specify Other:</b> <input type="text"/>                                    |

What is the scientific or technical purpose and importance of the proposed research? (limit : 500 words)



## Answer the 6 important questions

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What is the scientific or technical purpose and importance of the proposed research? (limit: 500 words)

Why do you need the APS for this research? (limit: 100 words)

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Why do you need the beamline you have chosen? (limit: 100 words)

## Answer the 6 important questions

What is the scientific or technical purpose and importance of the proposed research? (limit: 500 words)

Why do you need the APS for this research? (limit: 100 words)

Why do you need the beamline you have chosen? (limit: 100 words)

Describe the participants' previous experience with synchrotron radiation and the experimental results obtained. (If you refer to previous publications, be sure to include complete citations.) (limit: 100 words)

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Why do you need the beamline you have chosen? (limit: 100 words)

Describe the participants' previous experience with synchrotron radiation and the experimental results obtained. (If you refer to previous publications, be sure to include complete citations.) (limit: 100 words)

Describe samples and explain the proposed experiment, including procedures. Explain the basis for your estimated beam time needs. (limit: 500 words)

## Answer the 6 important questions

What is the scientific or technical purpose and importance of the proposed research? (limit: 500 words)

Why do you need the APS for this research? (limit: 100 words)

Why do you need the beamline you have chosen? (limit: 100 words)

Describe the participants' previous experience with synchrotron radiation and the experimental results obtained. (If you refer to previous publications, be sure to include complete citations.) (limit: 100 words)

Describe samples and explain the proposed experiment, including procedures. Explain the basis for your estimated beam time needs. (limit: 500 words)

Provide an overall estimate of the amount of beam time you will need to accomplish the goals of your proposed experimental program. How many visits during the two-year proposal period do you expect to need? How many shifts will you need during each visit (approximately)? (limit: 500 words)

# Select the review panel

The screenshot shows the Argonne National Laboratory website interface for the APS General User Proposal system. The top navigation bar includes 'Main Menu', 'Search Criteria', 'Instructions', and 'Logout'. Below this is a secondary navigation bar with tabs for 'General', 'Experimenters', 'Abstract', 'Beamtime Request', 'Questions', and 'Review Panel'. The 'Review Panel' tab is active.

The main content area displays the proposal ID 'GUP-30230' and contact information: 'General User Program: gu\_program@aps.anl.gov, 630-252-9090' and 'Technical assistance: mis\_mgrs@aps.anl.gov'. A green header bar contains this information.

The instruction reads: 'Please select the panel that you think is best suited to review your proposal. You may click [here](#) to see panel descriptions.'

The selection options are:

- Imaging/Microbeam
- Scattering - Applied Materials
- Scattering - Condensed Matter
- Scattering - Chem/Biol/Environ
- Small Angle Scattering (SAXS)
- Spectroscopy
- Instrumentation
- High Pressure
- 11-BM RA-mail-in

At the bottom of the selection area are 'Back' and 'Generate Report' buttons.

A final green bar contains instructions: 'Pressing SAVE will allow you to save this proposal and continue to make changes. Notifications will not be sent.' and 'Pressing SUBMIT will save this proposal AND notifications will be sent to the APS. No changes can be made thereafter.' It includes 'Save' and 'Submit' buttons.

The proposal ID 'GUP-30230' is repeated at the bottom of the green bar.

# Refractive optics

Just as with visible, light, it is possible to make refractive optics for x-rays



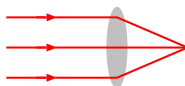
# Refractive optics

Just as with visible, light, it is possible to make refractive optics for x-rays

visible light:

$$n \sim 1.2 - 1.5$$

$$f \sim 0.1\text{m}$$



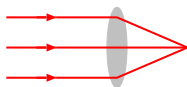
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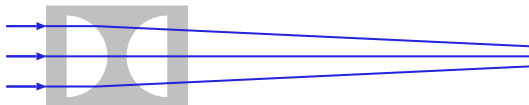
$$f \sim 0.1\text{m}$$



x-rays:

$$n \approx 1 - \delta, \delta \sim 10^{-5}$$

$$f \sim 100\text{m!}$$



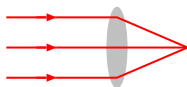
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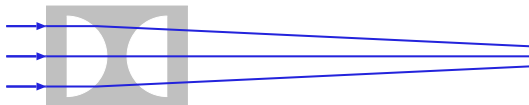
$$f \sim 0.1\text{m}$$



x-rays:

$$n \approx 1 - \delta, \delta \sim 10^{-5}$$

$$f \sim 100\text{m!}$$



x-ray lenses are complementary to those for visible light

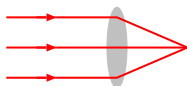
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visible light:

$$n \sim 1.2 - 1.5$$

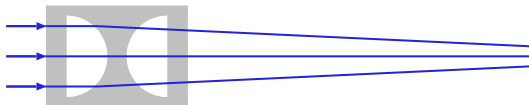
$$f \sim 0.1\text{m}$$



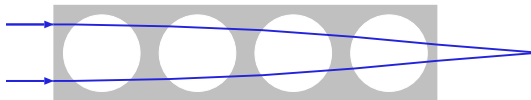
x-rays:

$$n \approx 1 - \delta, \delta \sim 10^{-5}$$

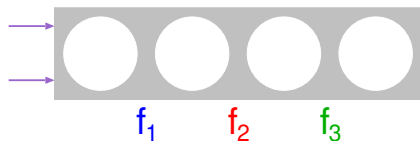
$$f \sim 100\text{m!}$$



x-ray lenses are complementary to those for visible light  
getting manageable focal distances requires making compound lenses

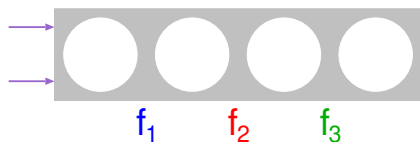


## Focal length of a compound lens



Start with a 3-element compound lens, calculate effective focal length

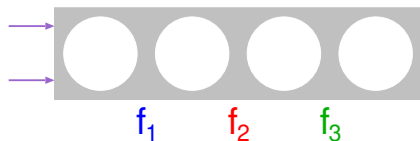
## Focal length of a compound lens



$$\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$$

Start with a 3-element compound lens, calculate effective focal length assuming each lens has the same focal length,  $f$

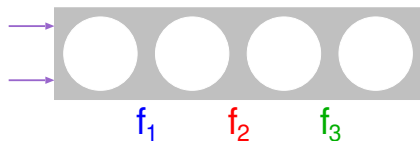
## Focal length of a compound lens



$$\frac{1}{i} + \frac{1}{o} = \frac{1}{f} \rightarrow \frac{1}{i} = \frac{1}{f} - \frac{1}{o}$$

Start with a 3-element compound lens, calculate effective focal length assuming each lens has the same focal length,  $f$

## Focal length of a compound lens



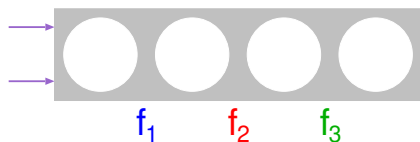
$$\frac{1}{i} + \frac{1}{o} = \frac{1}{f} \rightarrow \frac{1}{i} = \frac{1}{f} - \frac{1}{o}$$

$$\frac{1}{i_1} = \frac{1}{f_1} - \frac{1}{o_1}$$

Start with a 3-element compound lens, calculate effective focal length assuming each lens has the same focal length,  $f$



## Focal length of a compound lens



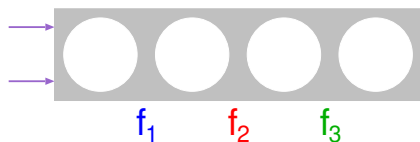
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$$f_1 = f, o_1 = \infty$$

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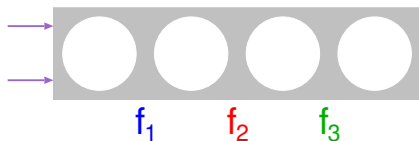
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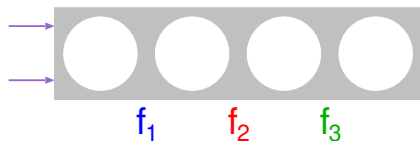
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for the second lens, the image  $i_1$  is a virtual object,  $o_2 = -i_1$

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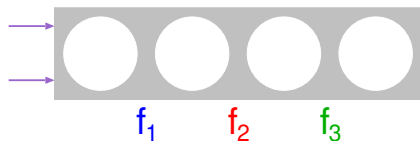
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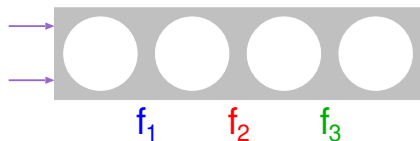
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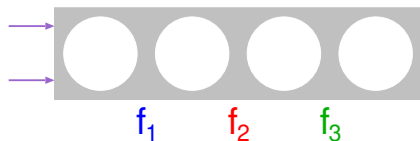
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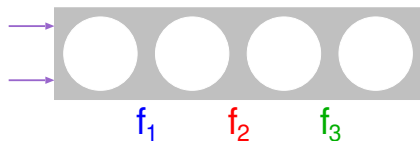
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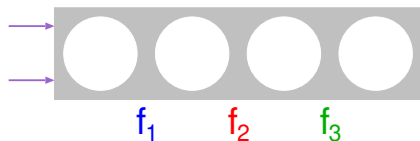
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so for N lenses  $f_{\text{eff}} = f/N$

## Rephasing distance

A spherical surface is not the ideal lens as it introduces aberrations. Derive the ideal shape for perfect focusing of x-rays.

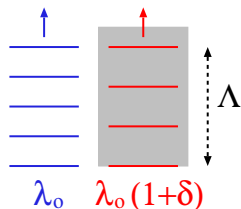
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 $\lambda = \lambda_0/(1 - \delta) \approx \lambda_0(1 + \delta)$

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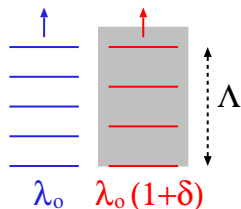
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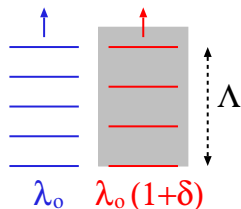
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if the two waves start in phase, they will be in phase once again after a distance

$$\Lambda = (N + 1)\lambda_0 = N\lambda_0(1 + \delta)$$

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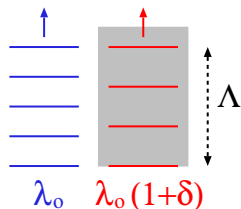
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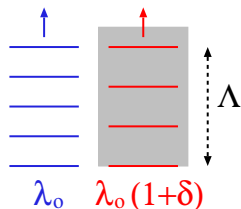
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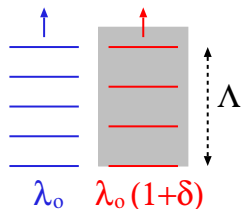
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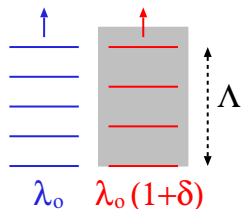
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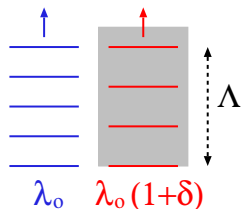
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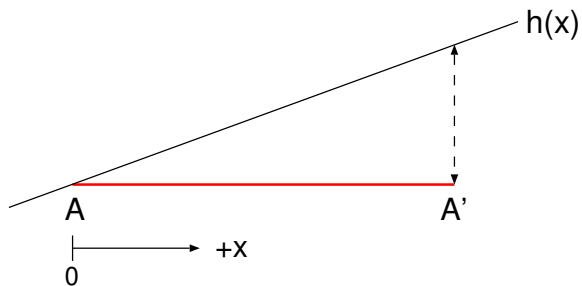
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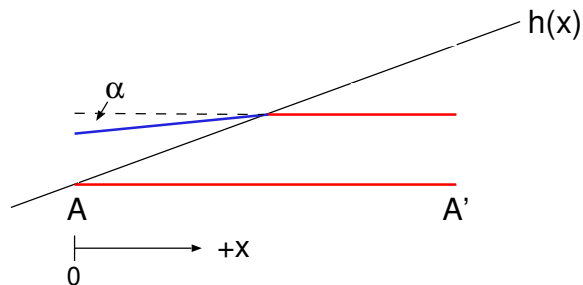
$$N\lambda_0 + \lambda_0 = N\lambda_0 + N\delta\lambda_0 \longrightarrow \lambda_0 = N\delta\lambda_0 \longrightarrow N = \frac{1}{\delta}$$

$$\Lambda = N\lambda_0 = \frac{\lambda_0}{\delta} = \frac{2\pi}{\lambda_0 r_0 \rho} \approx 10 \mu\text{m}$$

## Ideal interface profile - "thin" lens

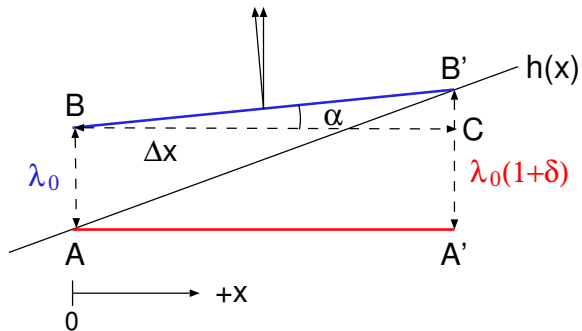


## Ideal interface profile - "thin" lens



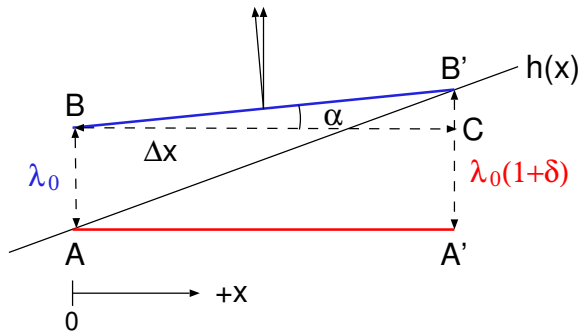
The wave exits the material into vacuum through a surface of profile  $h(x)$ , and is twisted by an angle  $\alpha$ .

## Ideal interface profile - "thin" lens



The wave exits the material into vacuum through a surface of profile  $h(x)$ , and is twisted by an angle  $\alpha$ . Follow the path of two points on the wavefront,  $A$  and  $A'$  as they propagate to  $B$  and  $B'$ .

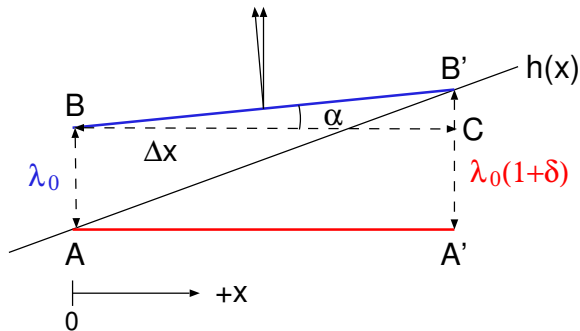
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from the  $AA'B'$  triangle

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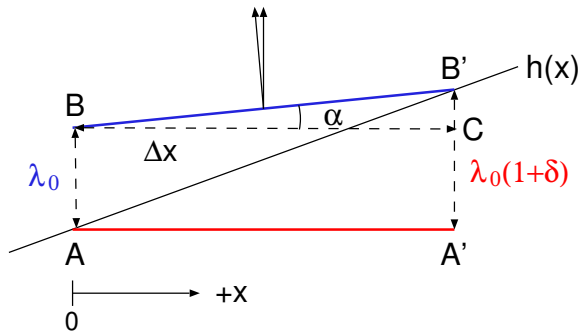
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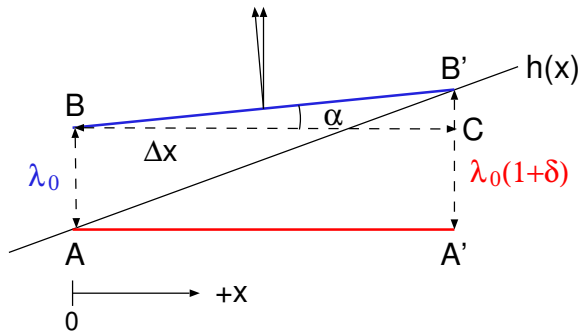


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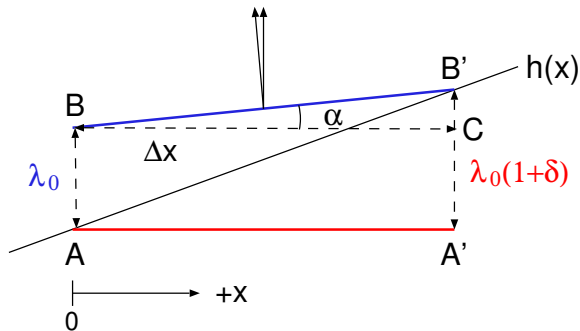
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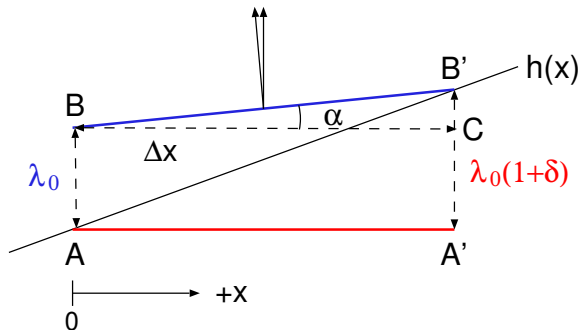
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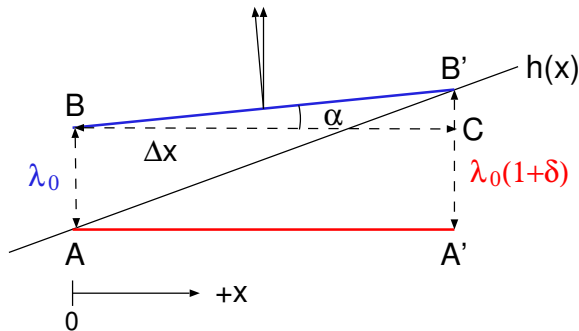
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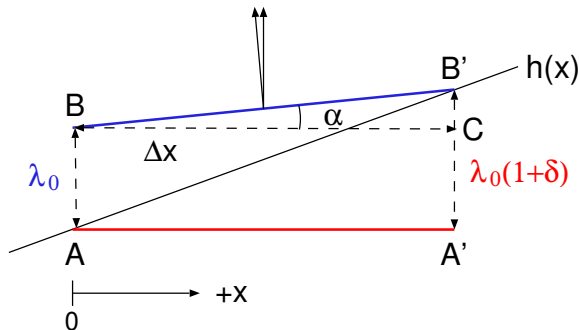
and from the  $BCB'$  triangle

using  $\Lambda = \lambda_0/\delta$

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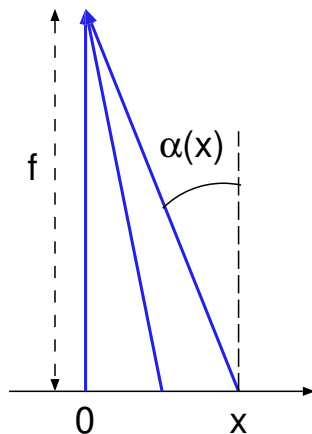
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## Ideal interface profile - “thin” lens

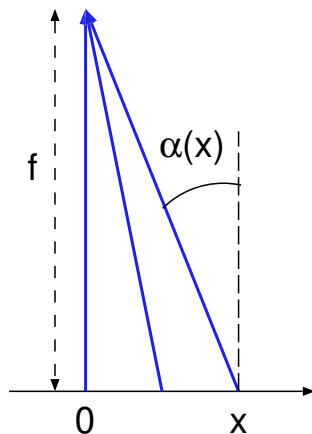
If the desired focal length of this lens is  $f$ , the wave must be redirected at an angle which depends on the distance from the optical axis



## Ideal interface profile - “thin” lens

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$$\alpha(x) = \frac{x}{f}$$





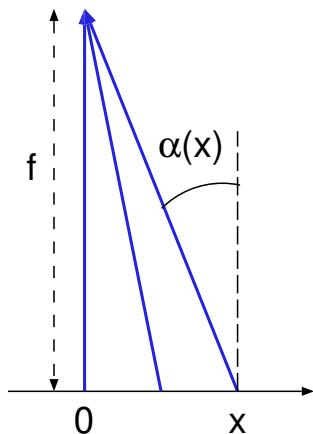
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$$\alpha(x) = \frac{x}{f}$$

combining, we have

$$\frac{\lambda_0 h'(x)}{\Lambda} = \frac{x}{f}$$



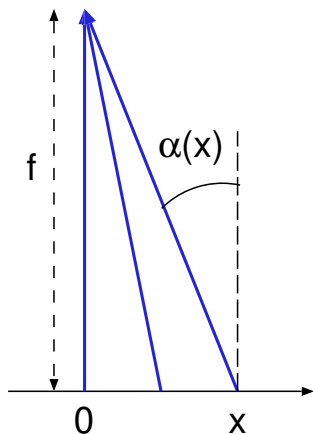
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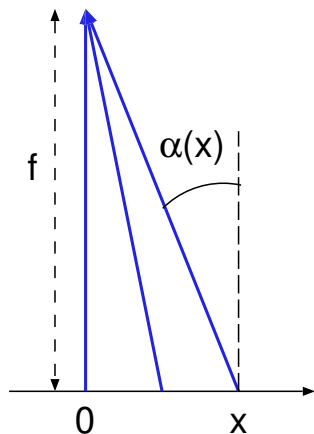
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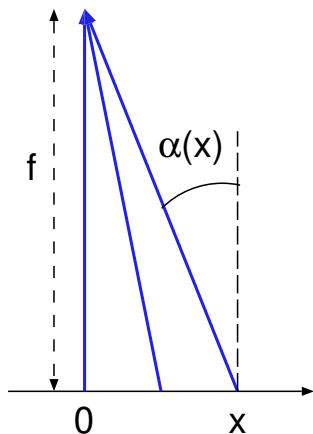
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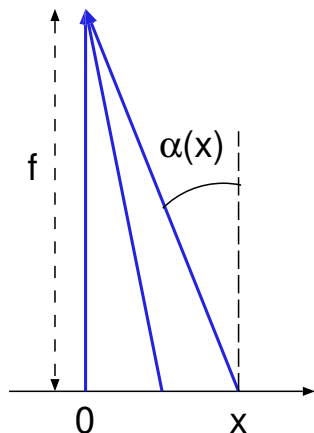
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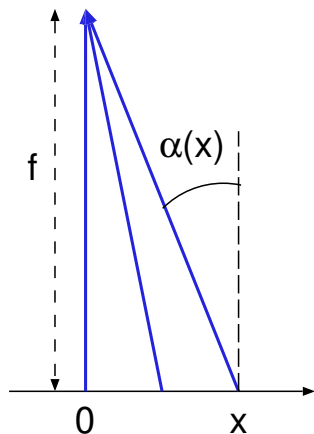
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a parabola is the ideal surface shape for focusing by refraction for a “thin” lens with limited aperture

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From the previous expression for the ideal parabolic surface, the focal length can be written in terms of the surface profile.

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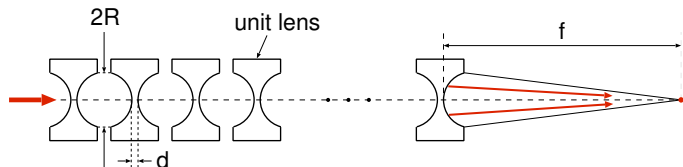
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for  $2N$  circular lenses we have

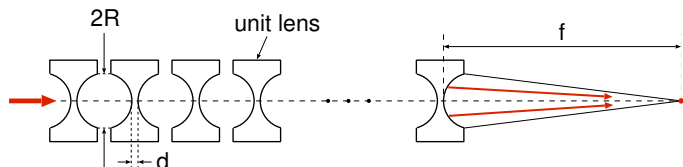
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# Focussing by a beryllium lens



H.R. Beguiristain et al., "X-ray focusing with compound lenses made from beryllium," *Optics Lett.*, **27**, 778 (2007).

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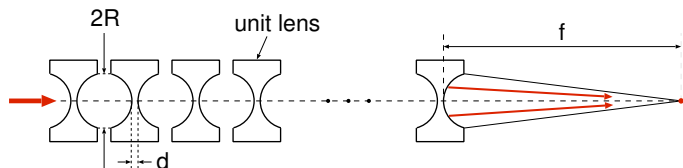


For 50 holes of radius  $R = 1\text{mm}$  in beryllium (Be) at  $E = 10\text{keV}$ , we can calculate the focal length, knowing  $\delta = 3.41 \times 10^{-6}$

$$f_N = \frac{R}{2N\delta}$$

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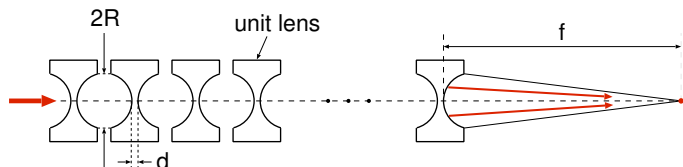


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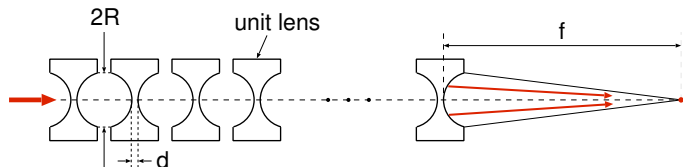


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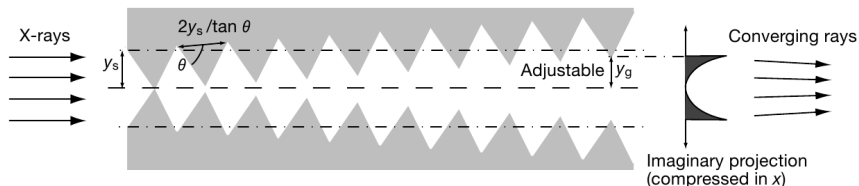
depending on the wall thickness of the lenslets, the transmission can be up to 74%

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## Alligator-type lenses

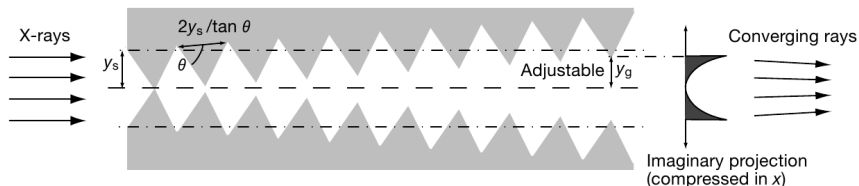
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This design has also been used to make lenses out of lithium metal.

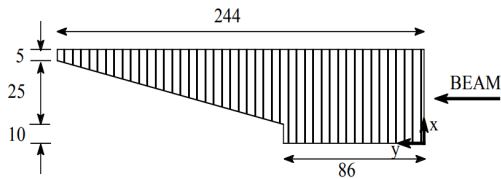
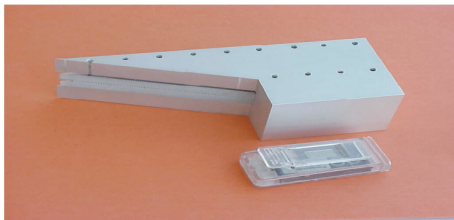
E.M. Dufresne et al., “Lithium metal for x-ray refractive optics”, *Appl. Phys. Lett.* **79**, 4085 (2001).

## Extruded Al lens

The compound refractive lenses (CRL) are useful for fixed focus but are difficult to use if a variable focal distance and a long focal length is required.

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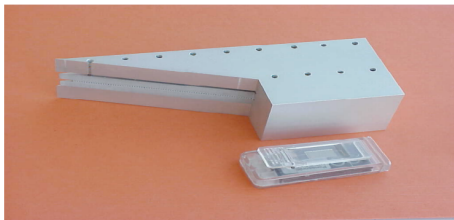
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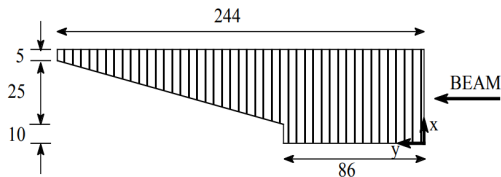
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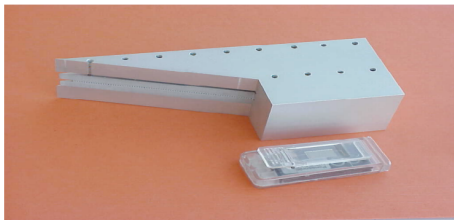
Extruded aluminum lens with parabolic figure



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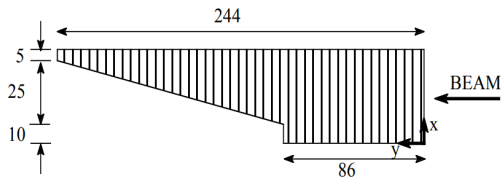
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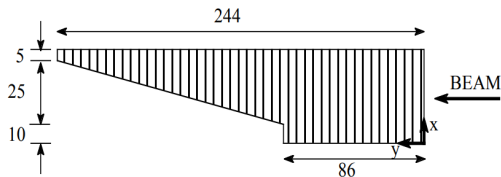
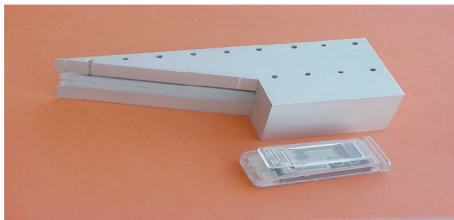
Cut diagonally to expose variable number of "lenses" to a horizontal beam



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Cut diagonally to expose variable number of "lenses" to a horizontal beam

Horizontal translation allows change in focal length but it is quantized, not continuous

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## Variable focal length CRL

A continuously variable focal length is very important for two specific reasons: tracking sample position, and keeping the focal length constant as energy is changed.

B. Adams and C. Rose-Petruck, "X-ray focusing scheme with continuously variable lens," *J. Synchrotron Radiation* **22**, 16-22 (2015).



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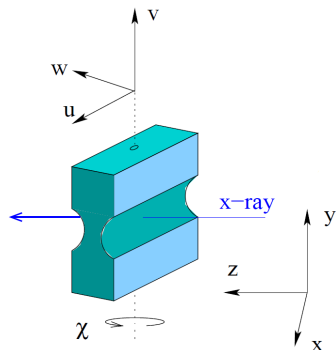
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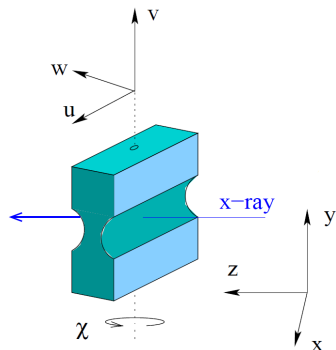


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Start with a 2 hole CRL. Rotate by an angle  $\chi$  about vertical axis

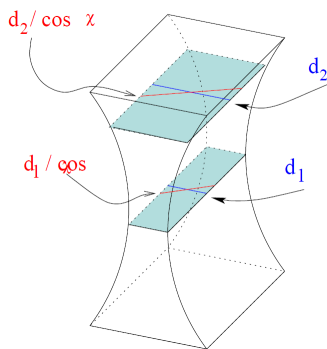


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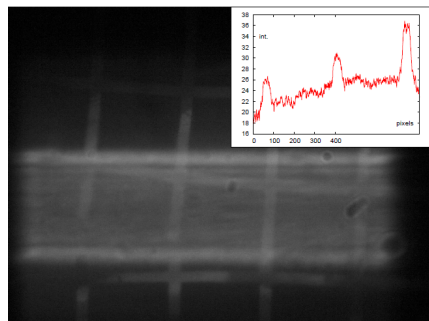
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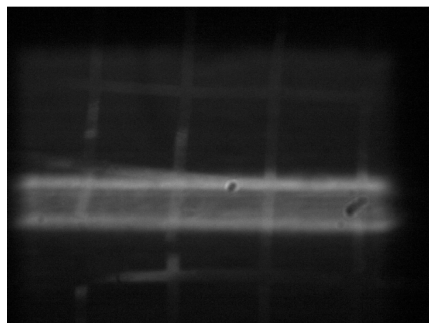
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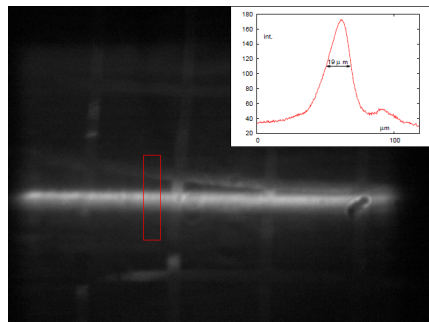
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Optimal focus is  $20\mu\text{m}$  at  $\chi = 40^\circ$



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