

Today's outline - January 28, 2020

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- Undulator harmonics

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Reading Assignment: Chapter 3.1–3.3

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Reading Assignment: Chapter 3.1–3.3

Homework Assignment #01:

Chapter 2: 2,3,5,6,8

due Thursday, January 30, 2020

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Now let us look at the coherence of the undulator radiation

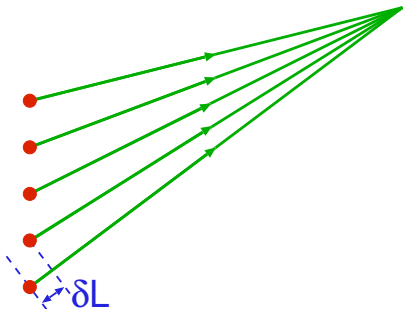
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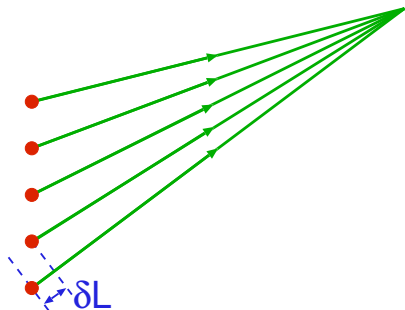
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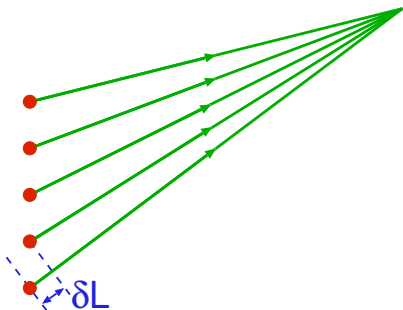


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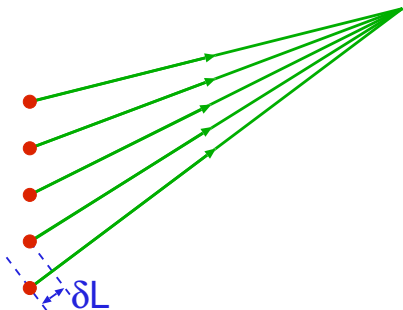


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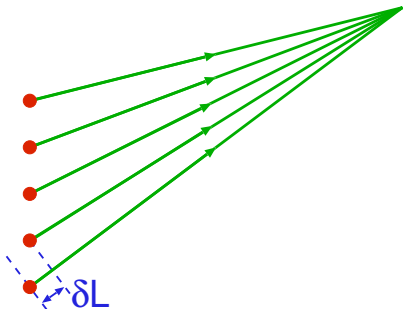


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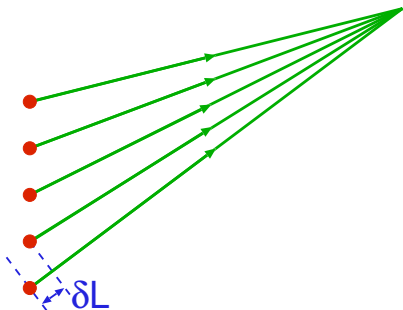
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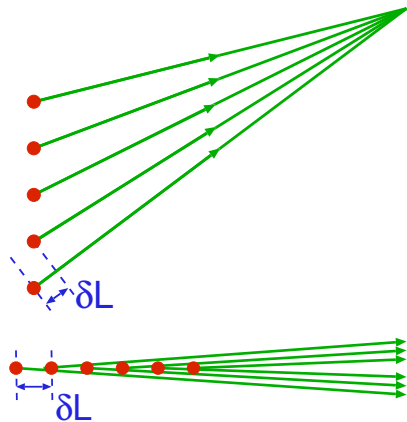
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the phase shift from each undulator pole depends on the wavelength λ_u

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$$I = \frac{\sin^2(\pi N\epsilon)}{\sin^2(\pi\epsilon)}$$

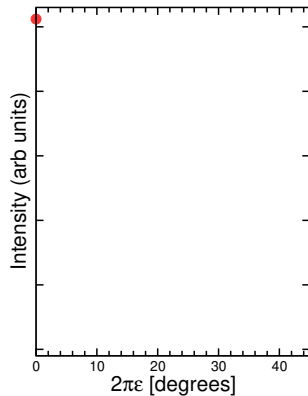
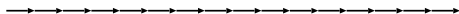
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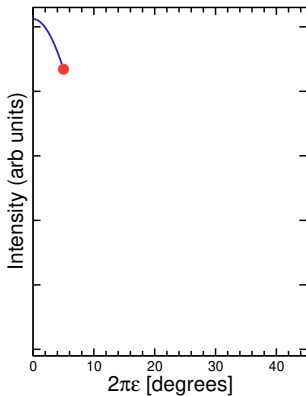
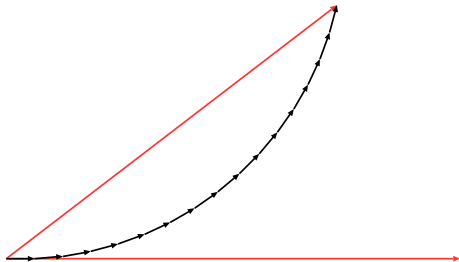
$$2\pi\epsilon=0$$



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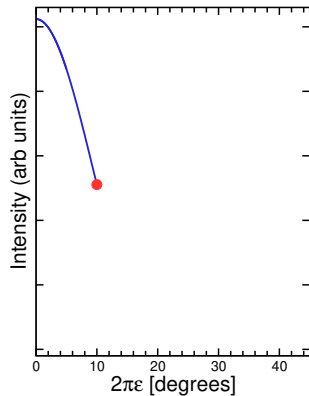
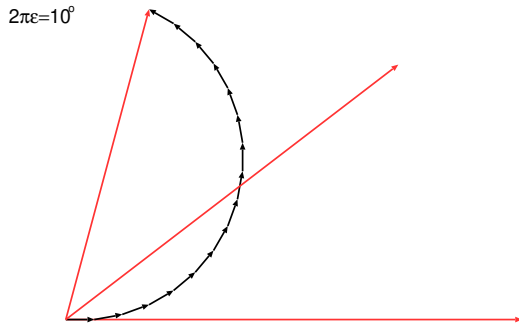
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$$2\pi\epsilon = 5^\circ$$



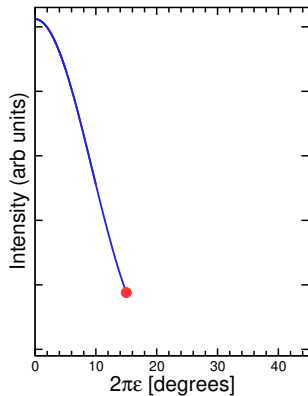
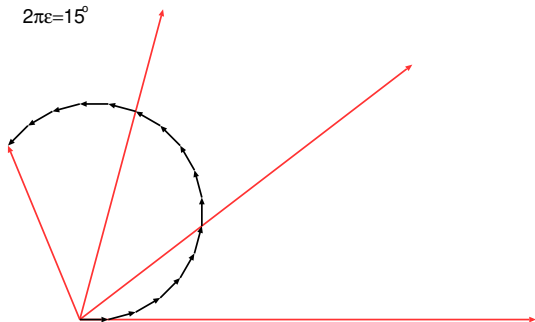
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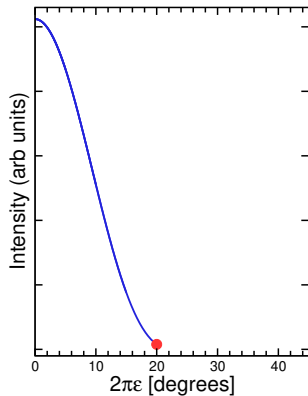
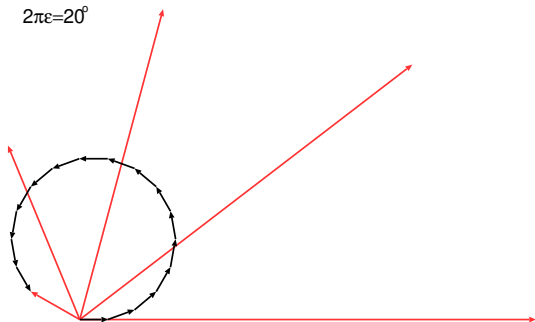
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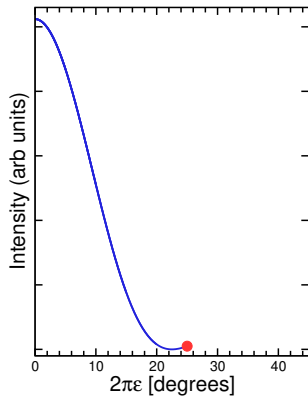
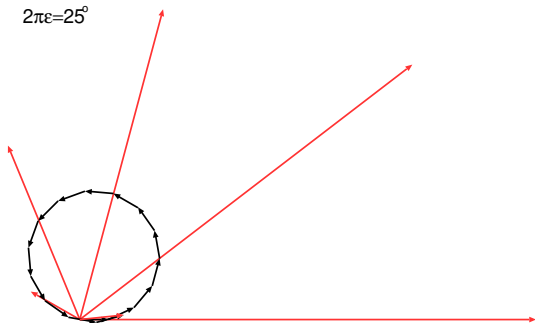
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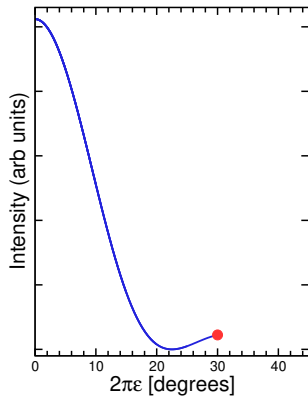
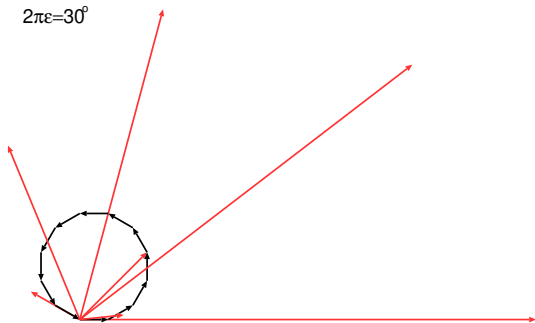
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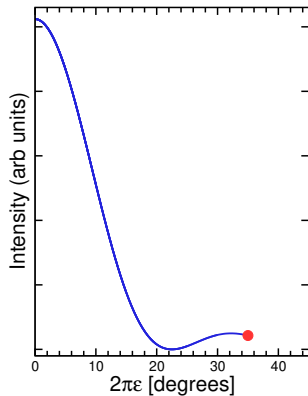
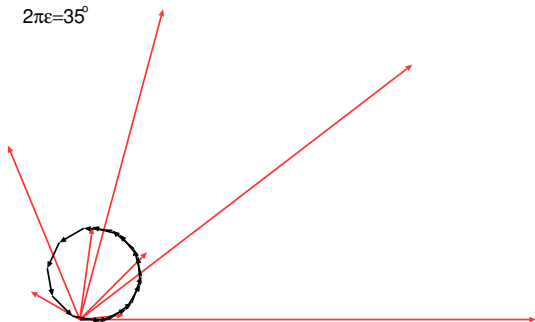
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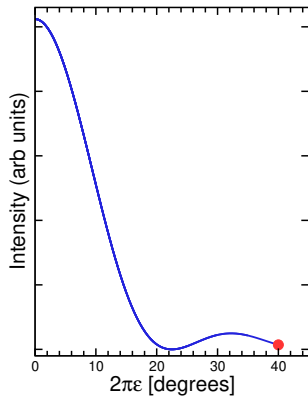
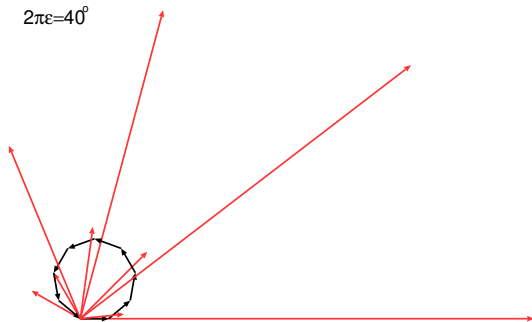
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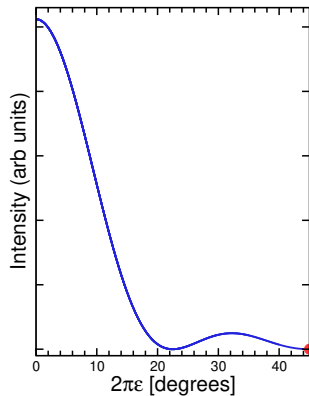
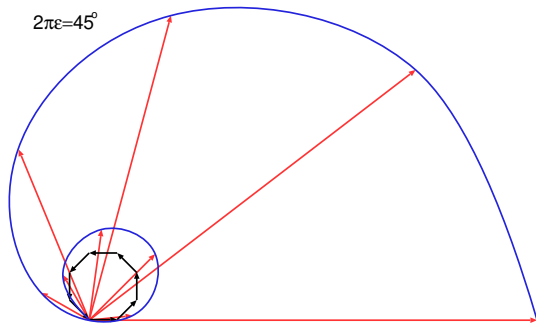
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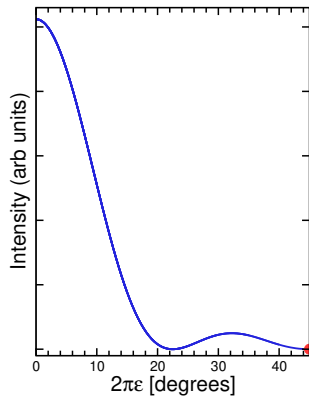
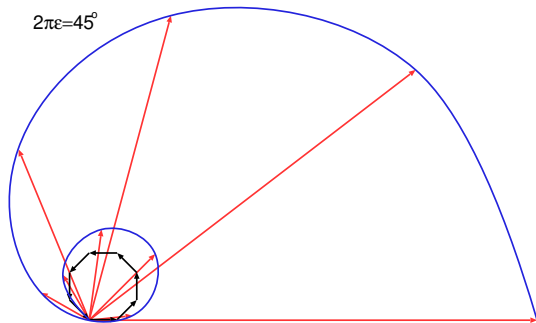
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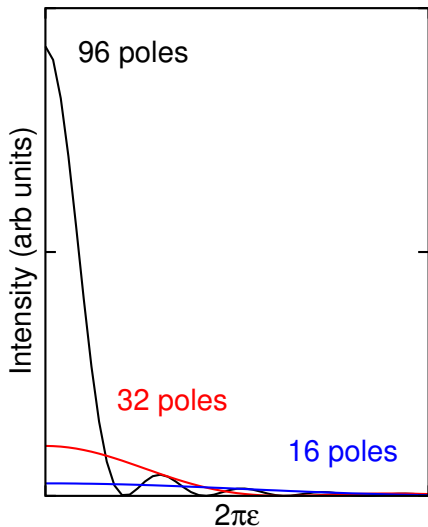
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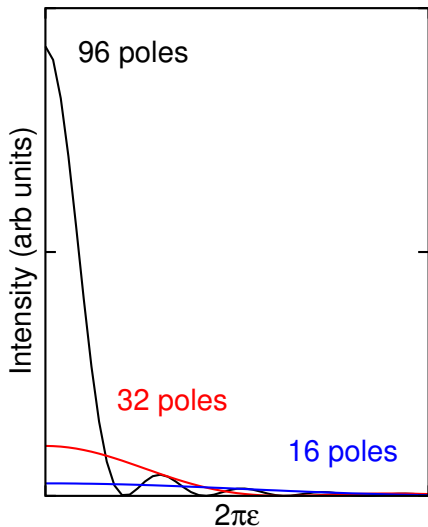
With the height and width of the peak dependent on the number of poles.

Undulator monochromaticity



The more poles in the undulator, the more monochromatic the beam since a slight change in $\epsilon = \delta L/\lambda$ implies a slightly different wavelength λ

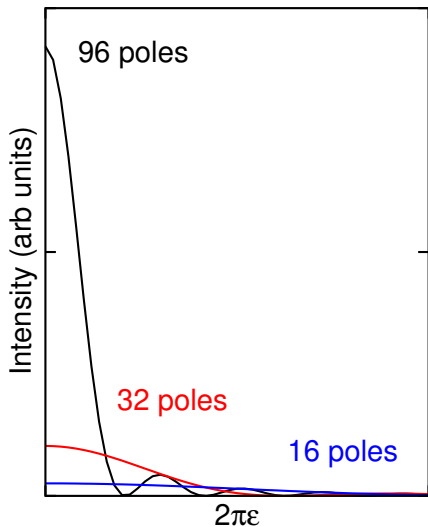
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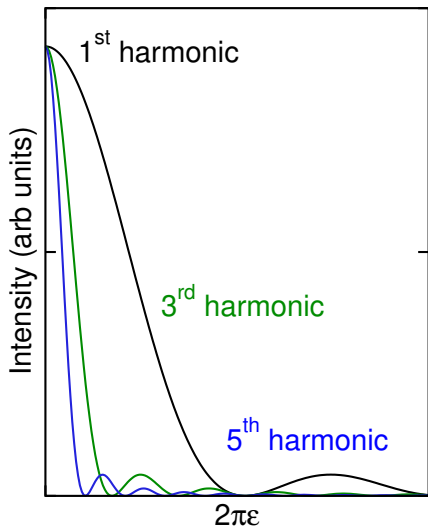


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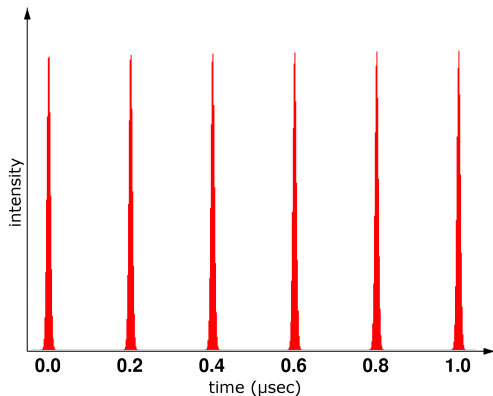
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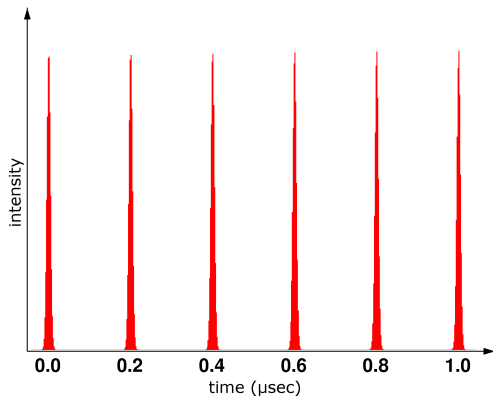
Higher order harmonics have narrower energy bandwidth but lower peak intensity

Synchrotron time structure



There are two important time scales for a storage ring such as the APS: pulse length and interpulse spacing

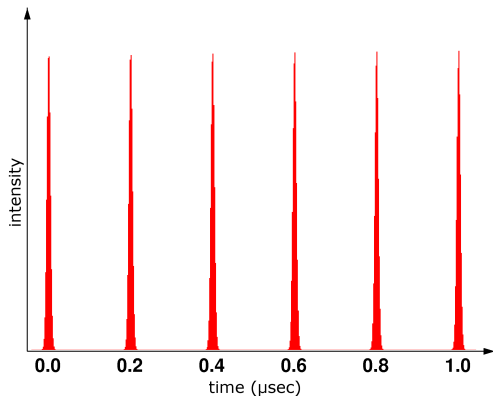
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Other modes include single-bunch mode for timing experiments and 324-bunch mode (inter pulse timing of 11.7 ns) for a more constant x-ray flux

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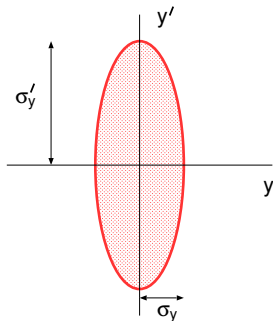
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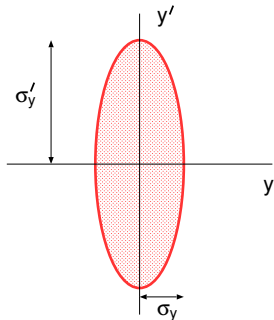
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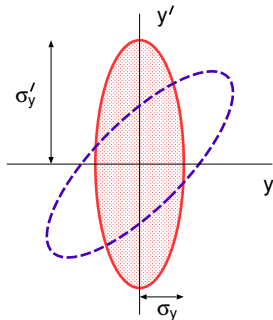
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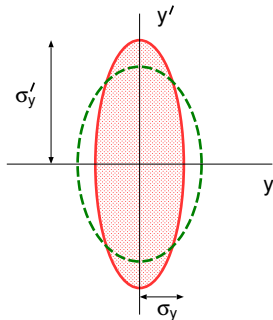
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this **emittance** cannot be changed but it can be **rotated** or **deformed** by magnetic fields as the electron beam travels around the storage ring as long as the area is kept constant



APS emittance

For photon emission from a single electron in a 2m undulator at 1\AA

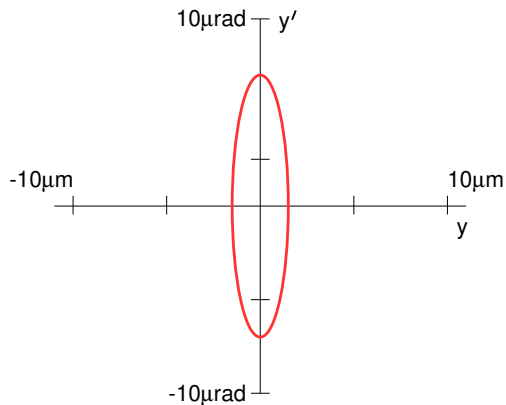
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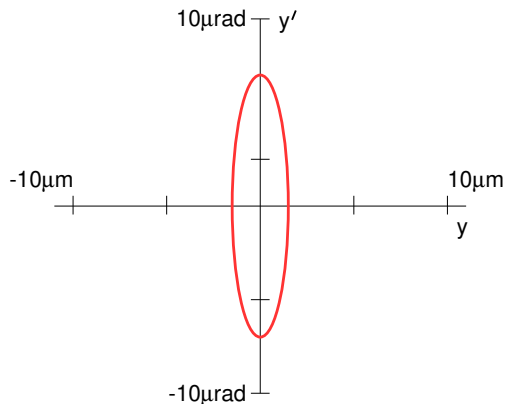
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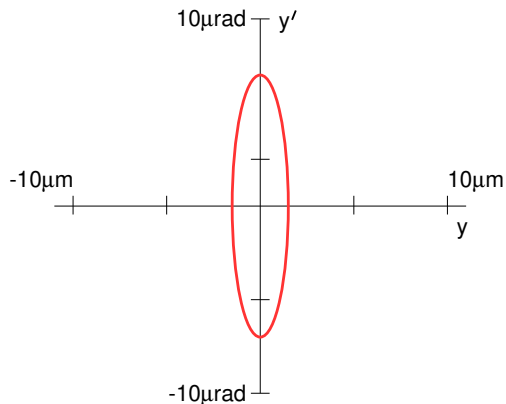
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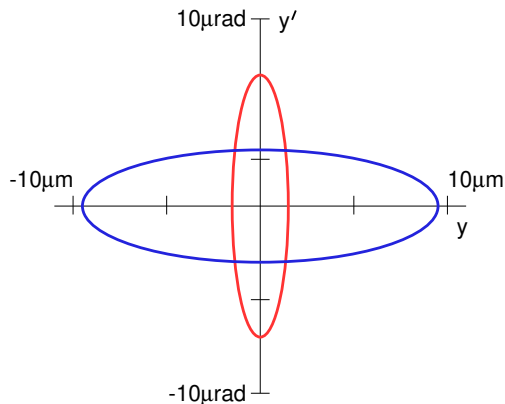
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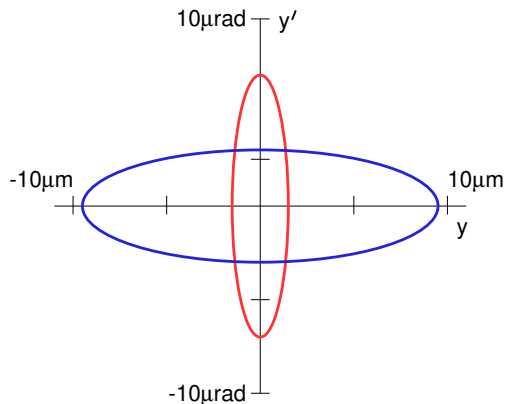
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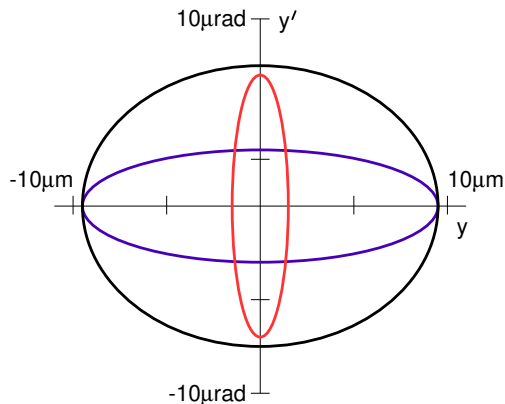
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The next big upgrade (slated for 2022) will make the beam more square in space and by choosing the undulator correctly, a higher performance insertion device.

APS upgrade

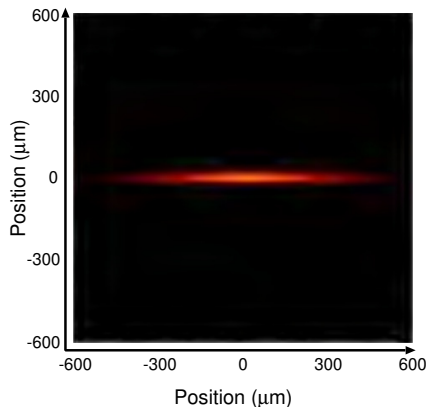
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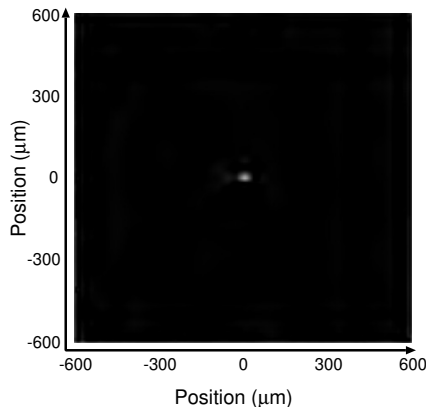
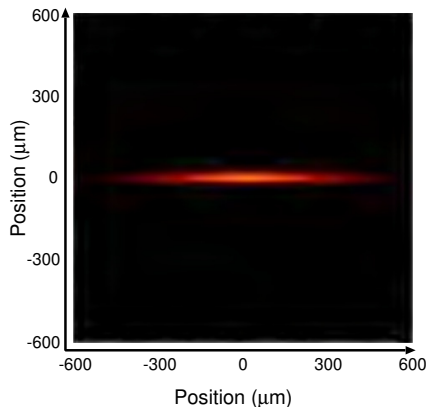
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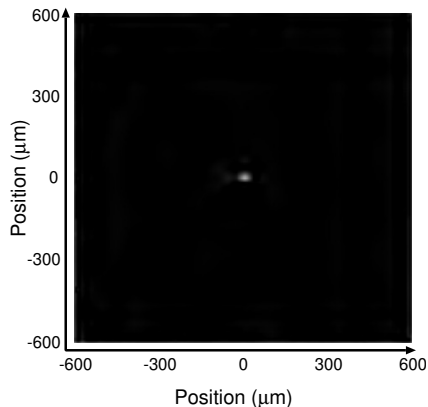
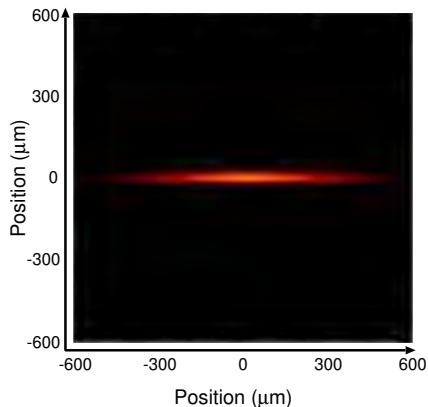
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The beam will be nearly square and there will be much more coherence from the undulators

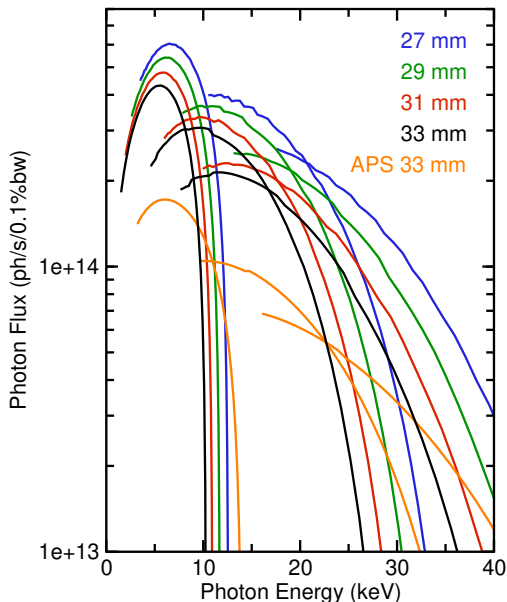
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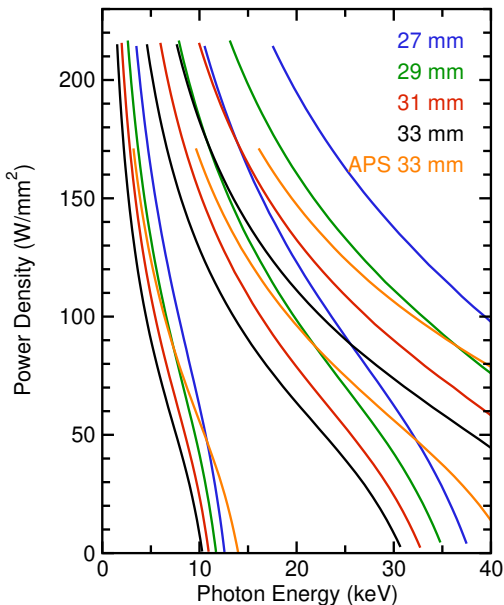


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The APS is calling this a "4th" generation synchrotron source



Energy recovery linacs

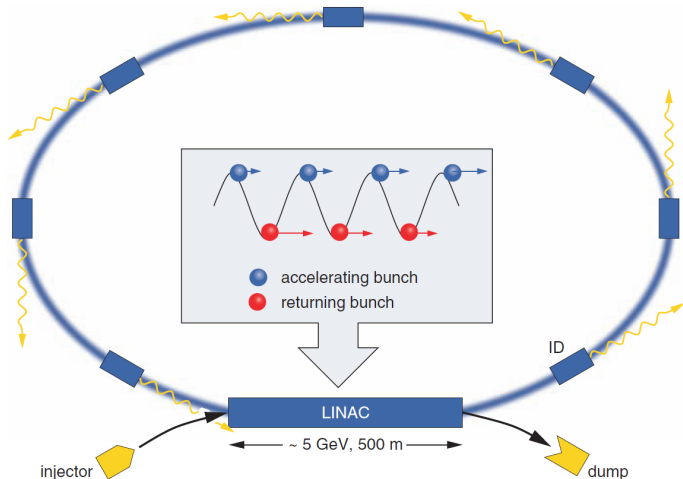
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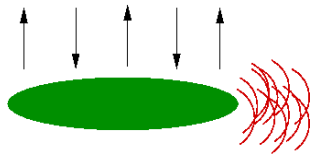
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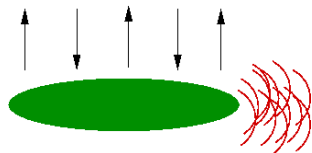
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Free electron laser

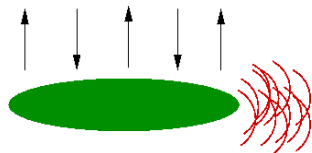


Free electron laser



Initial electron cloud, each electron emits coherently but independently

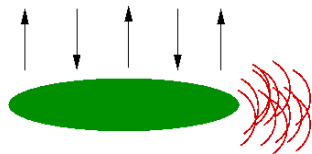
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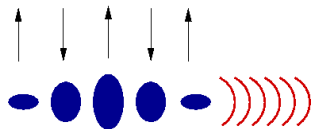
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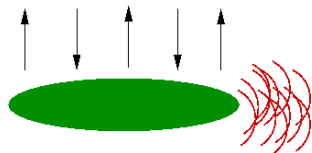


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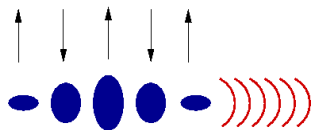


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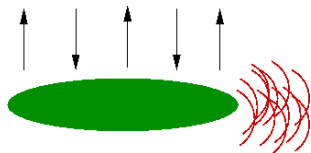
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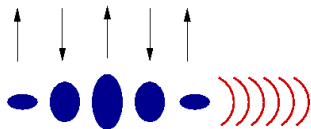
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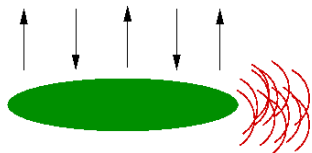
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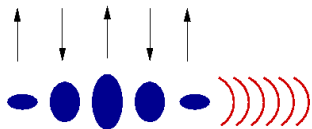
Each microbunch emits coherently with neighboring ones

Free electron laser



Initial electron cloud, each electron emits coherently but independently

Over course of 100 m, electric field of photons, feeds back on the electron bunch

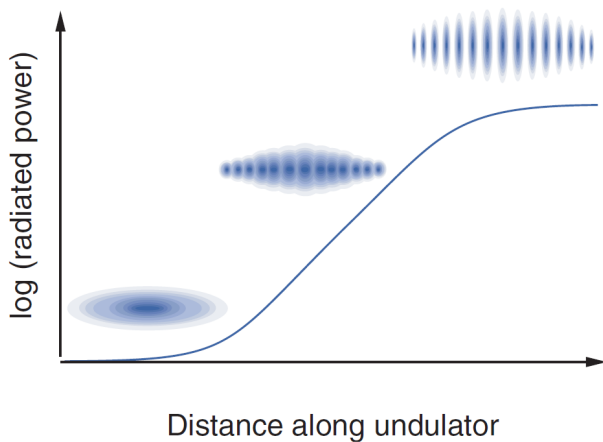


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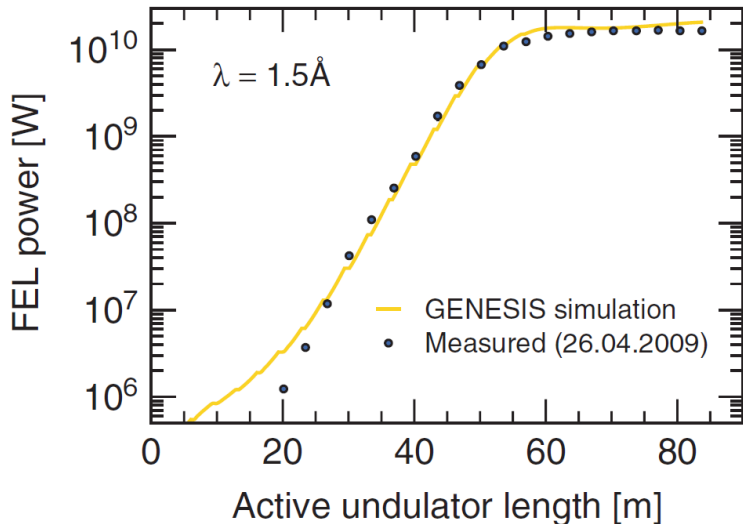
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Again, an alternative way to view this is that the pulse train from a 100m long undulator is long enough in time to produce a monochromatic and coherent frequency distribution when Fourier Transformed

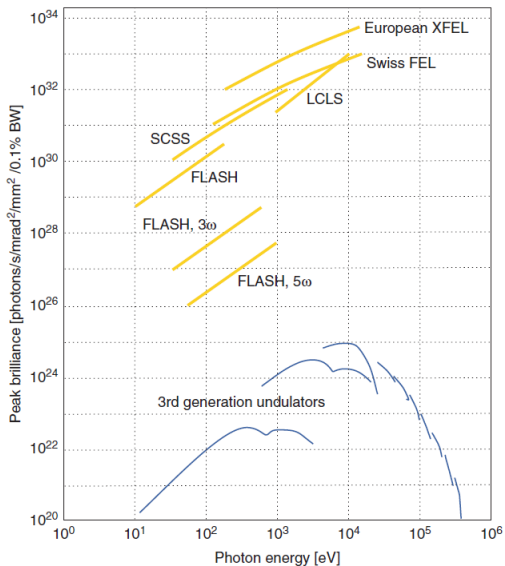
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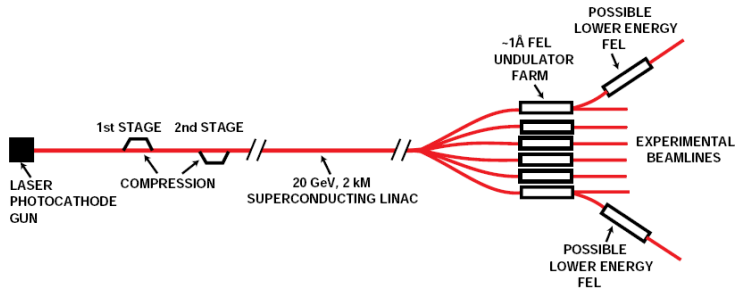
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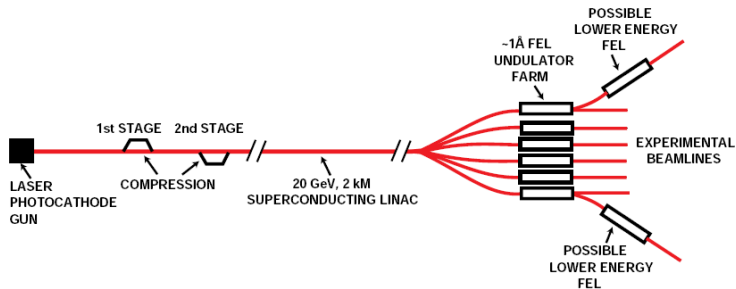
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FEL layout

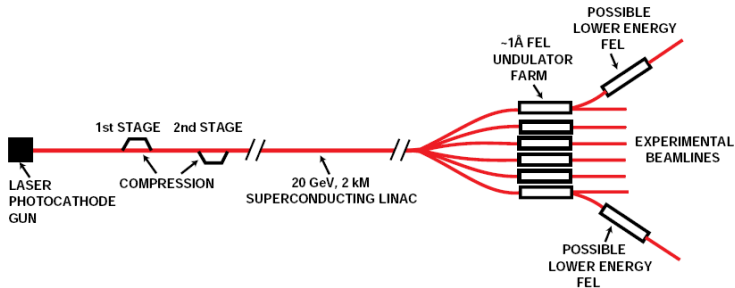


FEL layout



An FEL has a single accelerator whose electron beam is shunted sequentially through different undulators and end stations

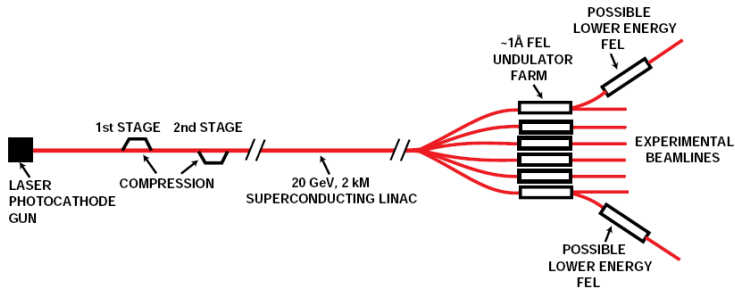
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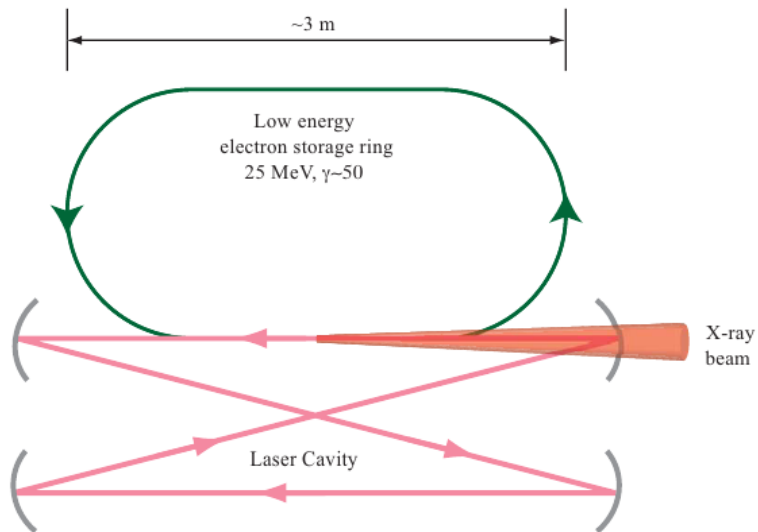


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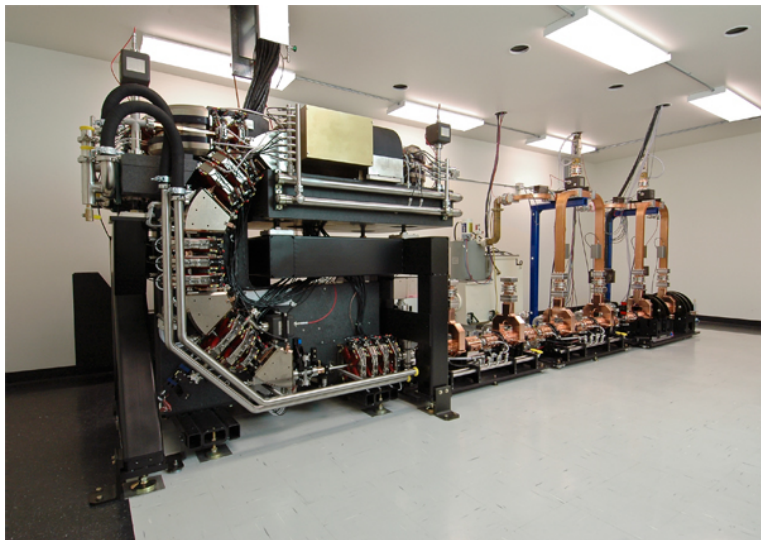
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The high brightness usually results in destruction of the sample during the illumination, thus the need for multiple samples and multiple shot experiments

Compact sources



Lyncean CLS



Types of X-ray Detectors

Types of X-ray Detectors

Gas detectors

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Gas detectors

Scintillation counters

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Solid state detectors

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Charge coupled device detectors

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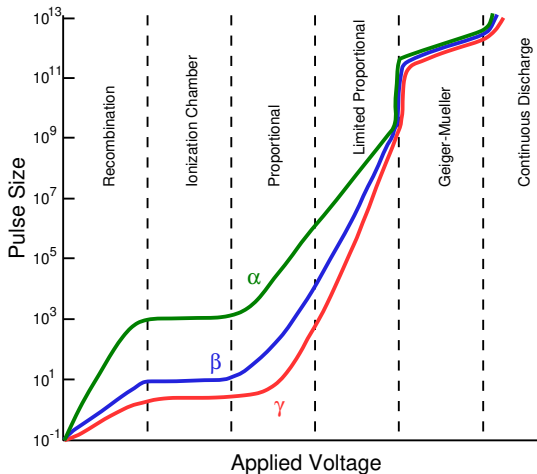
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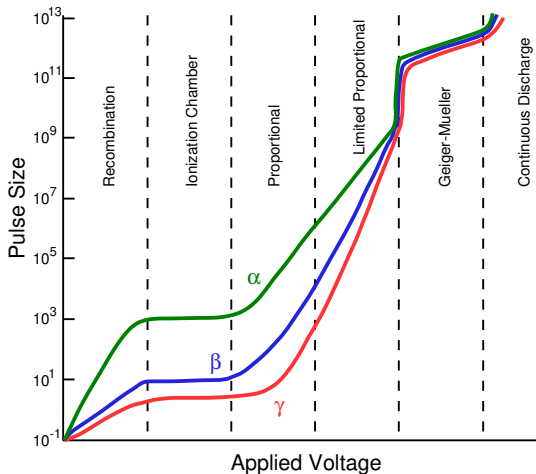
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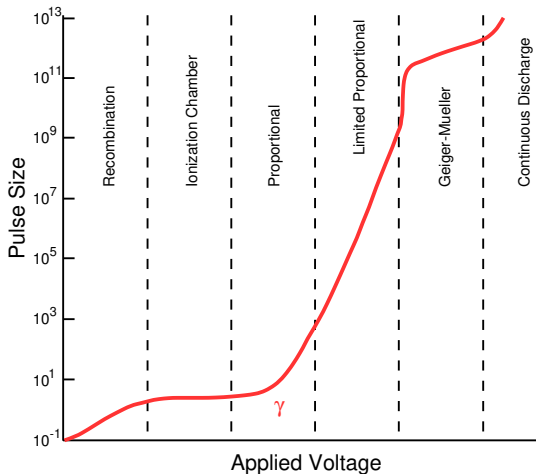


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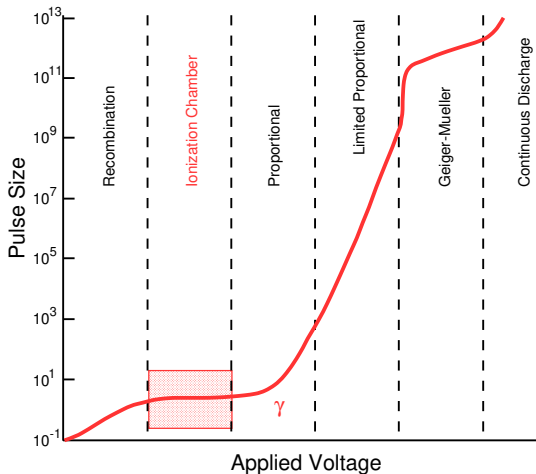
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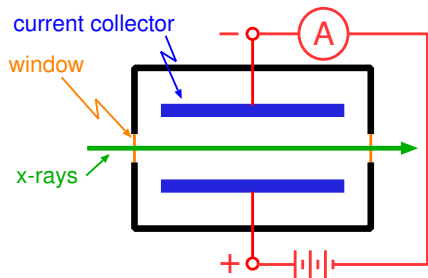
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The most useful regime is the ionization region where the output pulse is independent of the applied voltage over a wide range



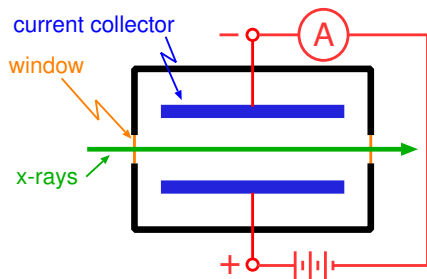
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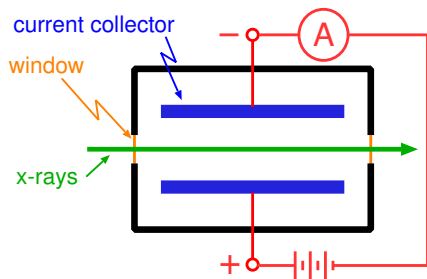


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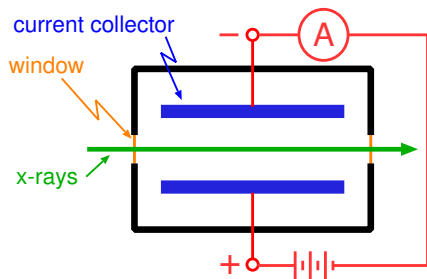
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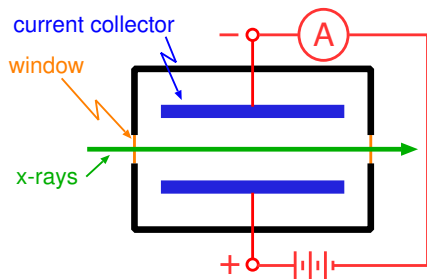
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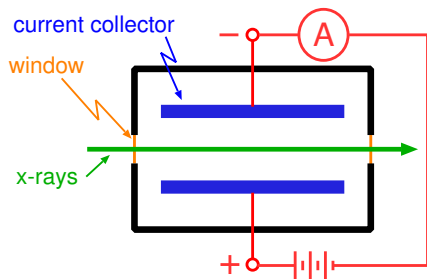
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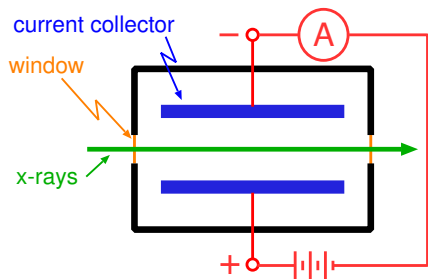


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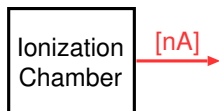


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- 22-41 eV per electron-ion pair (depending on the gas) makes this useful for quantitative measurements.

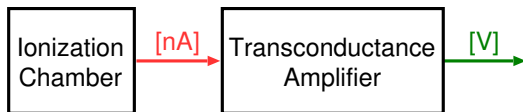
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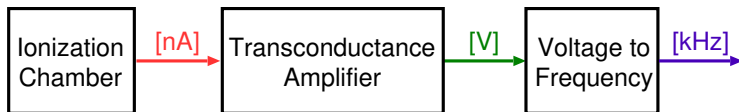
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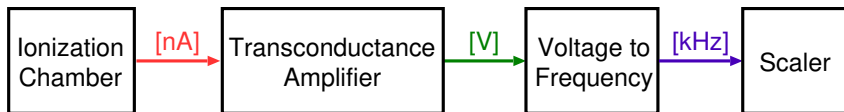


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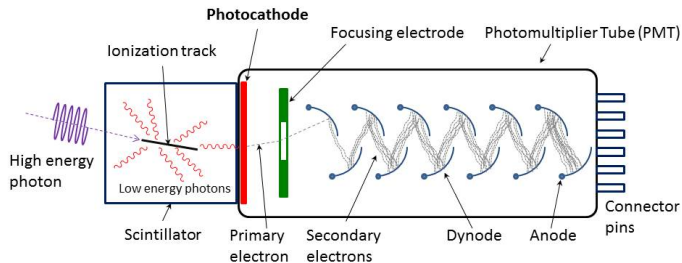
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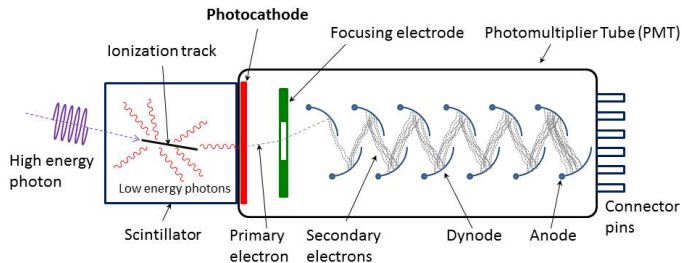
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Useful for photon counting experiments with rates less than $10^4/s$



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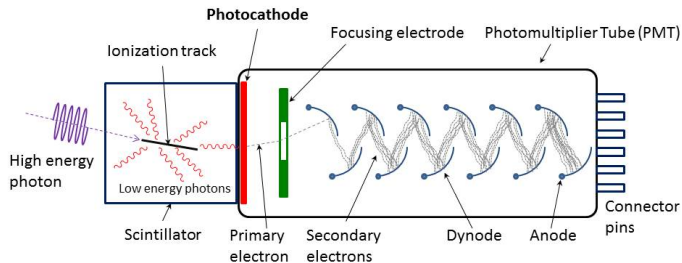
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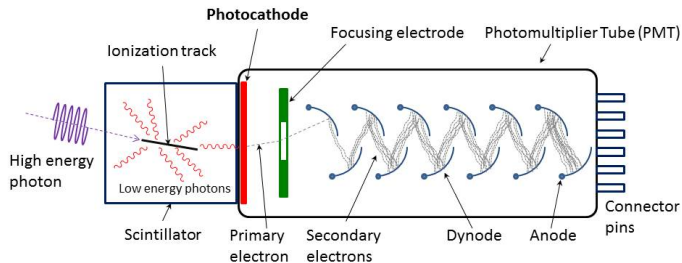
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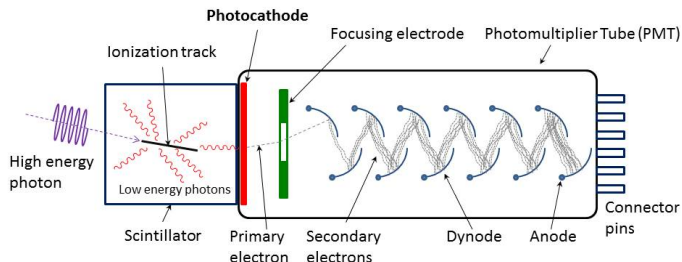
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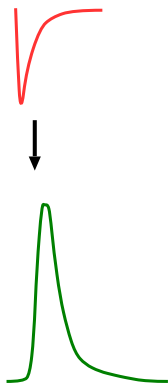
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- Output voltage pulse is proportional to initial x-ray energy.

Counting a scintillator pulse



the scintillator and photomultiplier put out a very fast negative-going **tail pulse** which is proportional to the energy of the photon

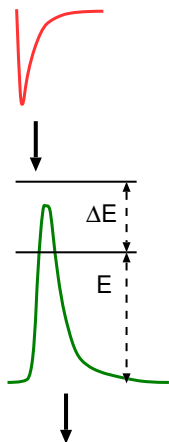
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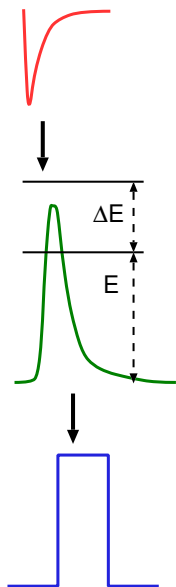
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if the **voltage pulse** falls within the discriminator window, a short **digital pulse** is output from the discriminator and into a scaler for counting

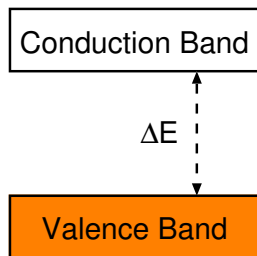
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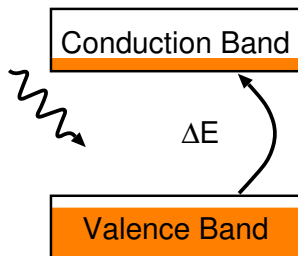


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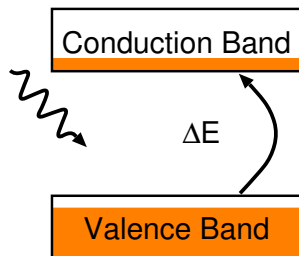
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because of the small energy required to produce an electron-hole pair, one x-ray photon will create many and its energy can be detected with very high resolution



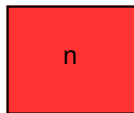
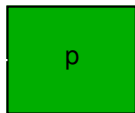
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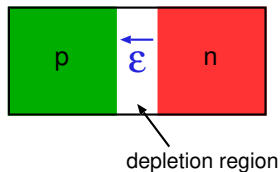


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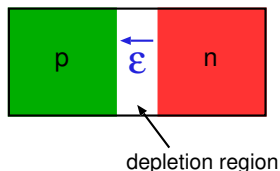


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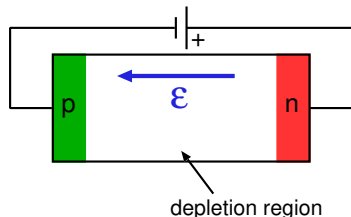
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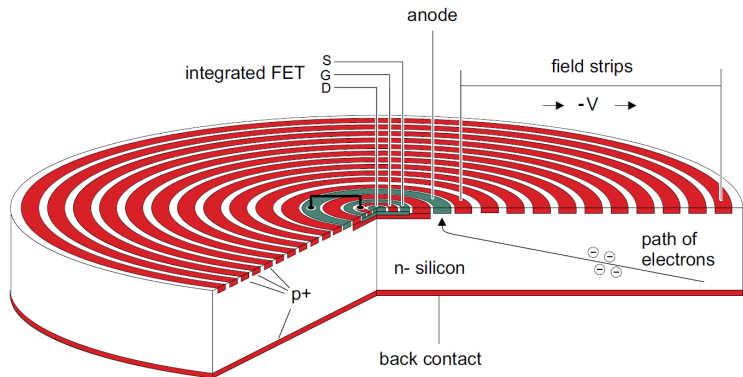
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by applying a reverse bias voltage, it is possible to extend the depleted region, make the effective volume of the detector larger and increase the **electric field** to get faster charge collection times



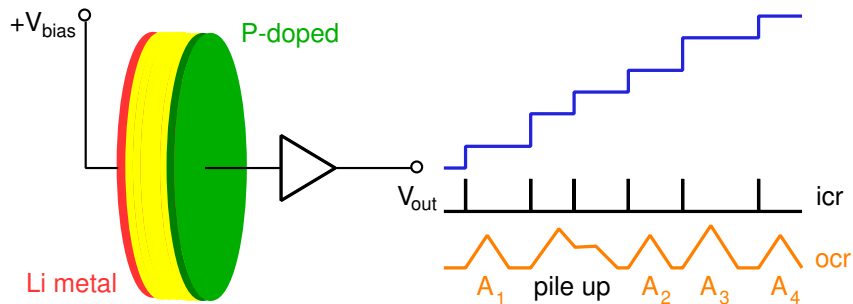
Silicon Drift Detector

Same principle as intrinsic or p-i-n detector but much more compact and operates at higher temperatures

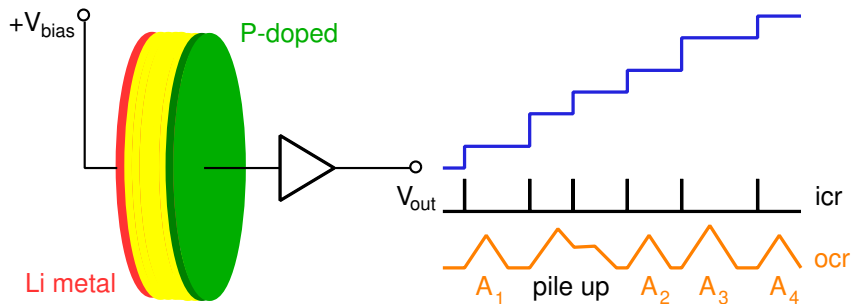


Relatively low stopping power is a drawback

Detector operation

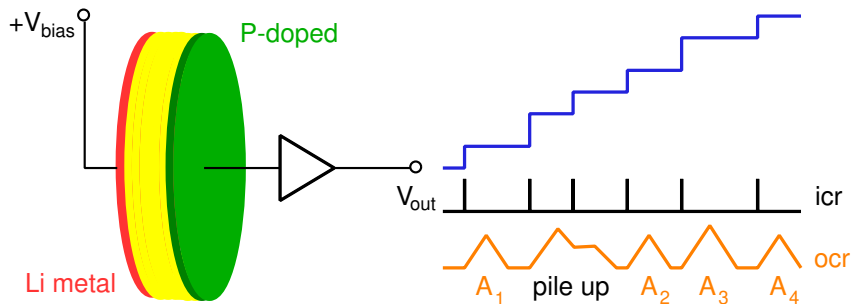


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output current is integrated into **voltage pulses** by a pre-amp, when maximum voltage is reached, output is optically reset

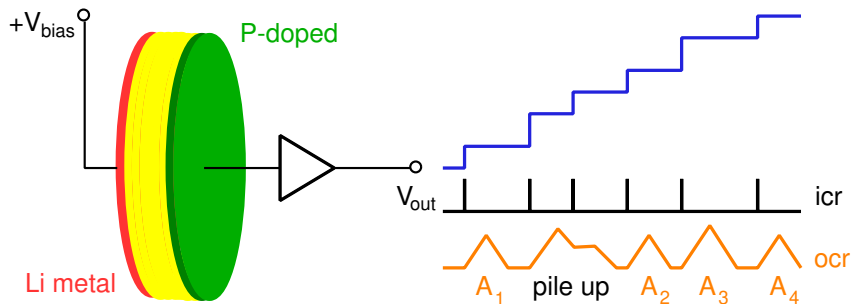
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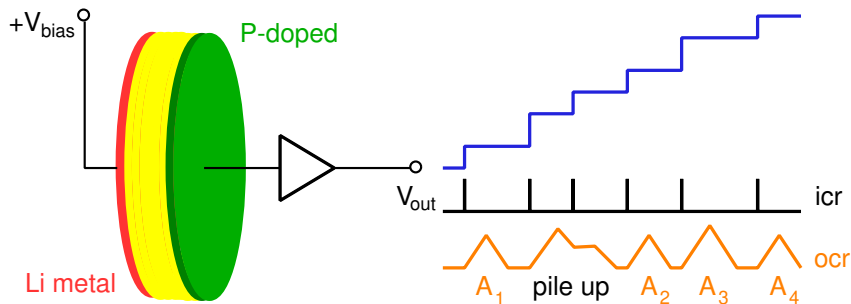
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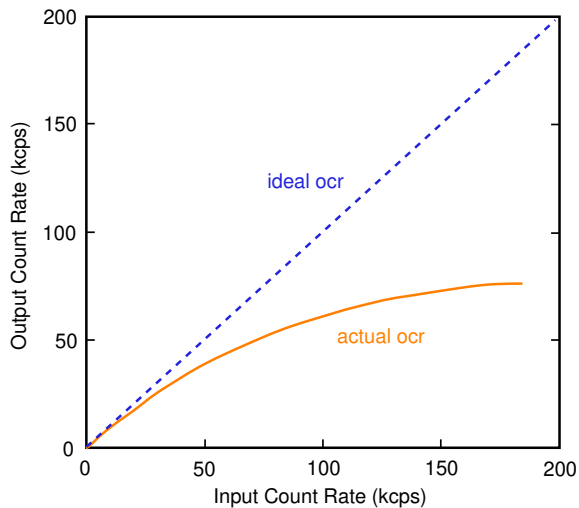


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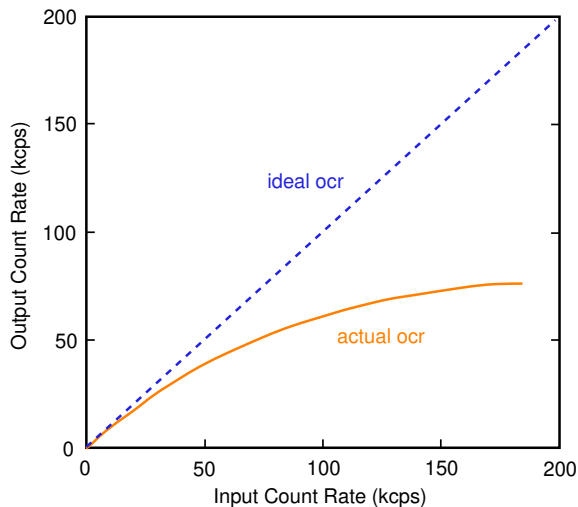
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electronics outputs input count rate (icr), output count rate (ocr), and areas of integrated pulses (A_n)

Dead time correction

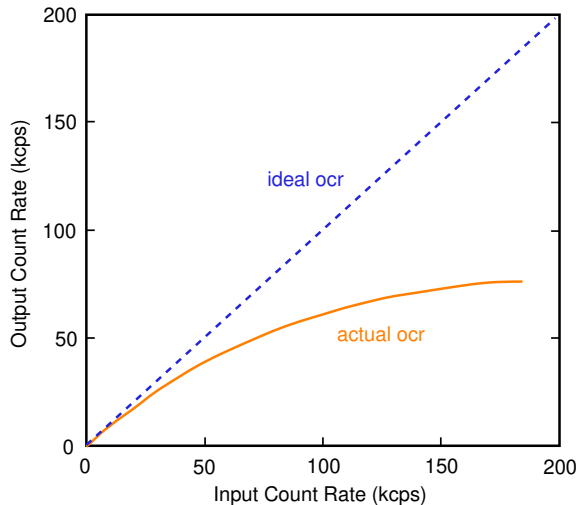


Dead time correction



the output count rate is significantly lower than the input count rate and gets worse with higher photon rate

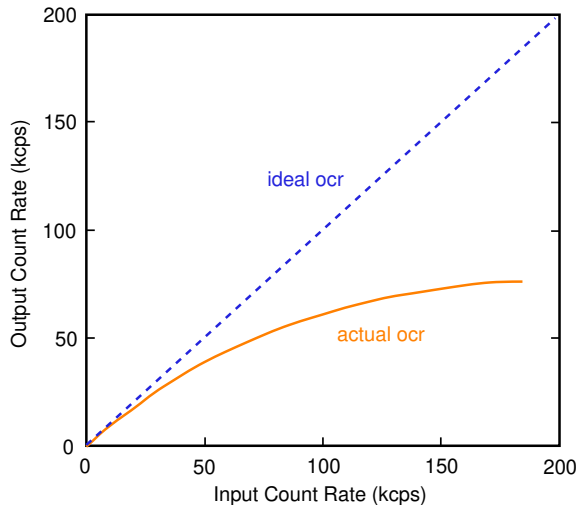
Dead time correction



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if these curves are known, a dead time correction can be applied to correct for roll-off

Dead time correction

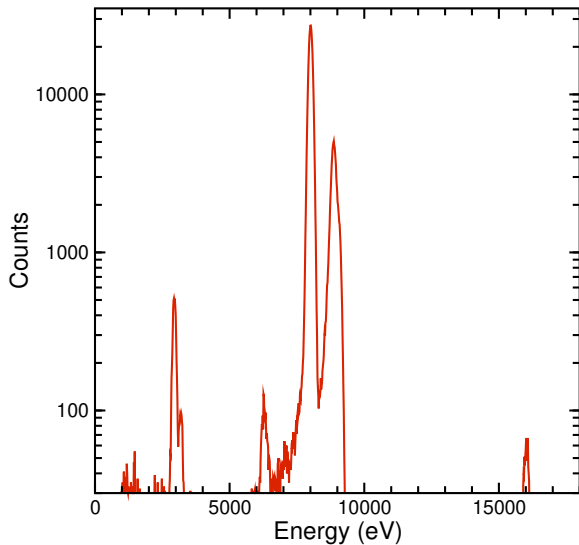


the output count rate is significantly lower than the input count rate and gets worse with higher photon rate

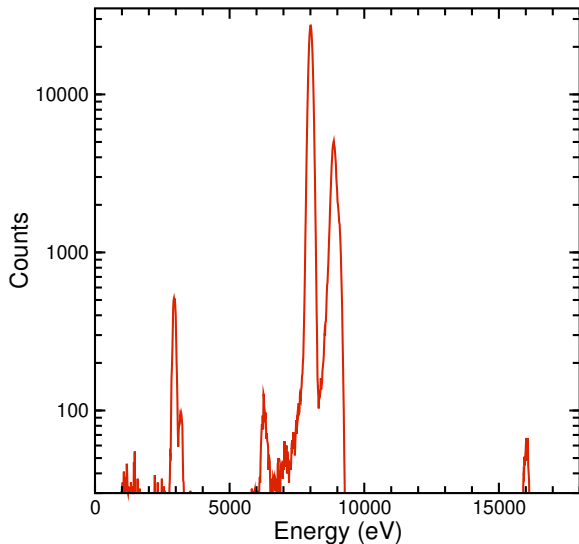
if these curves are known, a dead time correction can be applied to correct for roll-off

if dead time is too large, correction will not be accurate!

SDD spectrum

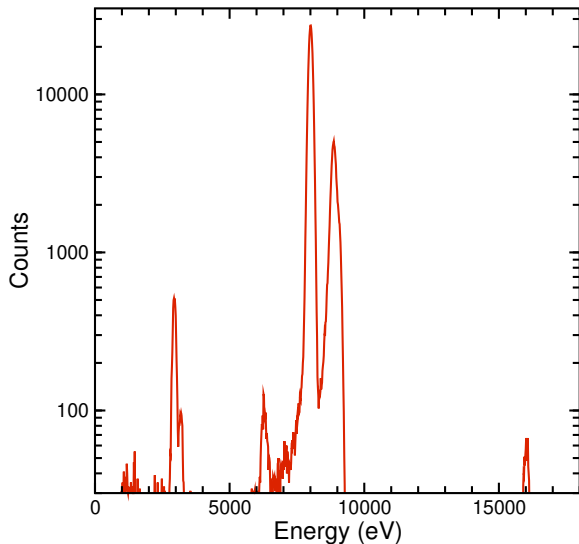


SDD spectrum



fluorescence spectrum
of Cu foil in air using
9200 eV x-rays

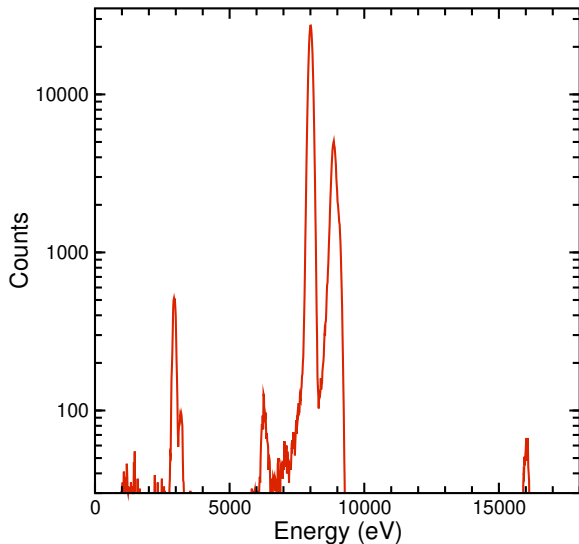
SDD spectrum



fluorescence spectrum
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9200 eV x-rays

Compton peak is visi-
ble just above the Cu
 K_{α} fluorescence line

SDD spectrum

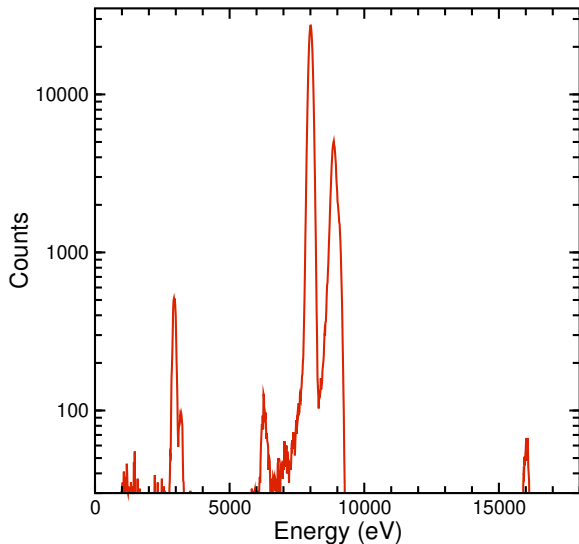


fluorescence spectrum
of Cu foil in air using
9200 eV x-rays

Compton peak is visi-
ble just above the Cu
 K_{α} fluorescence line

Ar fluorescence near
3000 eV

SDD spectrum



fluorescence spectrum
of Cu foil in air using
9200 eV x-rays

Compton peak is visi-
ble just above the Cu
 K_{α} fluorescence line

Ar fluorescence near
3000 eV

a small amount of
pulse pileup is visible
near 16000 eV