• Undulator coherence

- Undulator coherence
- ERLs and FELs

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Reading Assignment: Chapter 3.1–3.3

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Reading Assignment: Chapter 3.1–3.3

Homework Assignment #01: Chapter Chapter 2: 2,3,5,6,8 due Thursday, January 29, 2015

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$$\sum_{m=0}^{N-1} e^{i(\vec{k}\cdot\vec{r}+2\pi m\epsilon)} = e^{i\vec{k}\cdot\vec{r}} \sum_{m=0}^{N-1} e^{i2\pi m\epsilon}$$

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$$S_N - kS_N = 1 - k^N \quad \longrightarrow \quad S_N = \frac{1 - k^N}{1 - k}$$

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Therefore, for the diffraction grating we can calculate the intensity at the detector as

$$I = \left| e^{i\vec{k}\cdot\vec{r}} \sum_{m=0}^{N-1} e^{i2\pi m\epsilon} \right|^2 = \left| e^{i\vec{k}\cdot\vec{r}} S_N \right|^2 = \left| e^{i\vec{k}\cdot\vec{r}} \frac{\sin(\pi N\epsilon)}{\sin(\pi\epsilon)} e^{i\pi(N-1)\epsilon} \right|^2$$
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Beam coherence

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With the height and width of the peak dependent on the number of poles.

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Undulator coherence



Undulator coherence



Synchrotron time structure



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Energy recovery linacs

Undulators have limited peak brilliance

Energy recovery linacs

Undulators have limited peak brilliance but the use of an energy recovery linac can overcome this limitation and enhance peak brilliance by up to three orders of magnitude

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- Over course of 100 m, electric field of photons, feeds back on electron bunch



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- Microbunches form with period of FEL (and radiation in electron frame)

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- Over course of 100 m, electric field of photons, feeds back on electron bunch
- Microbunches form with period of FEL (and radiation in electron frame)
- Each microbunch emits coherently with neighboring ones

Self-amplified spontaneous emission



FEL emission



Distance along undulator

FEL emission



FEL emission



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Compact sources



Gas detectors

Gas detectors

Scintillation counters

Gas detectors

Scintillation counters Solid state detectors

Gas detectors

Scintillation counters Solid state detectors

Gas detectors

Ionization chamber

Scintillation counters Solid state detectors

Gas detectors

- Ionization chamber
- Proportional counter

Scintillation counters Solid state detectors

Gas detectors

- Ionization chamber
- Proportional counter
- Geiger-Muller tube
 Scintillation counters
 Solid state detectors
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Scintillation counters Solid state detectors

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Charge coupled device detectors

Indirect

Gas detectors

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Gas Detector Curve



Useful for beam monitoring, flux measurement, fluorescence measurement, spectroscopy.



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- Count rates up to 10¹¹ photons/s/cm³
- 22-41 eV per electron-hole pair (depending on the gas) makes this useful for quantitative measurements.

Useful for photon counting experiments



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• Nal(TI), Yttrium Aluminum Perovskite (YAP) or plastic which, absorb x-rays and fluoresce in the visible spectrum.

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- Output voltage pulse is proportional to initial x-ray energy.

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Solid State Detectors

Open circuit p-n junction has a natural depletion region



depletion region

Solid State Detectors

Open circuit p-n junction has a natural depletion region



When reverse biased, the depletion region grows

Solid State Detectors

Open circuit p-n junction has a natural depletion region



When reverse biased, the depletion region grows creating a higher electric field near the junction

Ge Detector Operation



Silicon Drift Detector

Same principle as intrinsic or p-i-n detector but much more compact and operates at higher temperatures



Relatively low stopping power is a drawback

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CCD detectors - direct



CCD detectors - indirect



CCD detectors - lightpipe taper



Pixel Array Detectors - schematic



Pixel Array Detectors - Pilatus



Pixel array detector with 1,000,000 pixels.

Each pixel has energy resolving capabilities & high speed readout.

Silicon sensor limits energy range of operation.

from Swiss Light Source

Pixel Array Detectors - high energy solutions

