

PHYS 407/507 & CS 495 - Introduction to Quantum Computing



Term: Spring 2026
Meetings: Tuesday & Thursday 17:00-18:15
Location: Room 117 Wishnick Hall
Video: All sessions recorded for online viewing

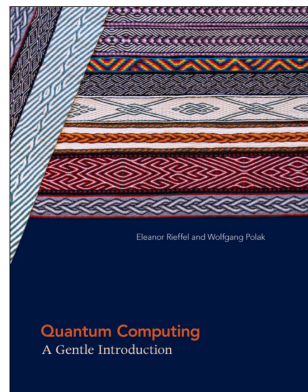
Instructor: Carlo Segre
Office: 166D/172 Pritzker Science
Phone: 312.567.3498
email: segre@illinoistech.edu

Resources: *Quantum Computing: A Gentle Introduction*,
E. Rieffel & W. Polak (MIT Univ Press, 2011)

Introduction to Classical and Quantum Computing,
T. Wong (Rooted Grove, 2022)

Quirk: A drag-and-drop quantum circuit simulator, Craig Gidney

Web Site: <http://phys.iit.edu/~segre/phys407/26S>



Course objectives for PHYS 407/507 & CS 495



1. Clearly describe the building blocks of quantum computing.

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1. Clearly describe the building blocks of quantum computing.
2. Apply tools of quantum computing to manipulate qubits.

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5. Use the concept of quantum entanglement to develop quantum algorithms.

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7. Build quantum algorithms using Quirk.
8. Demonstrate the programming of a quantum computer using Python.

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4. Clearly describe the purpose and realization of quantum gates.
5. Use the concept of quantum entanglement to develop quantum algorithms.
6. Clearly describe the techniques of quantum error correction and fault tolerance.
7. Build quantum algorithms using Quirk.
8. Demonstrate the programming of a quantum computer using Python.
9. Successfully program an agreed-upon quantum algorithm on an IBM quantum computer.



- Homework Assignments

Course syllabus



- Homework Assignments
- Qiskit Progress Reports



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- Qiskit Progress Reports
- Midterm Exams – Online, handwritten uploads to Canvas



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- Final Exam – Presentations on research articles
 - Choose a recent research article which features a synchrotron technique
 - Get approval before starting
 - Timetable will be posted



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 - Choose a recent research article which features a synchrotron technique
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 - Timetable will be posted
- Final project - programming a quantum algorithm
 - Start thinking about a suitable project right away
 - Make proposal and get approval before starting



PHYS 407 & CS 495

PHYS 507

Course grading



PHYS 407 & CS 495

30% – Homework assignments

PHYS 507

20% – Homework assignments



PHYS 407 & CS 495

30% – Homework assignments
Weekly, due at beginning of class

PHYS 507

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PHYS 407 & CS 495

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Turned in via Canvas

PHYS 507

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PHYS 407 & CS 495

- 30% – Homework assignments
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- 40% – Exams

PHYS 507

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PHYS 407 & CS 495

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- 40% – Exams
- 30% – Final presentation

PHYS 507

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- 40% – Exams
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- 20% – Final project



PHYS 407 & CS 495

30% – Homework assignments
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40% – Exams

30% – Final presentation

Grading scale

A	–	88%	to	100%
B	–	75%	to	88%
C	–	62%	to	75%
D	–	50%	to	62%
E	–	0%	to	50%

PHYS 507

20% – Homework assignments
Weekly, due at beginning of class
Turned in via Canvas

40% – Exams

20% – Final presentation

20% – Final project

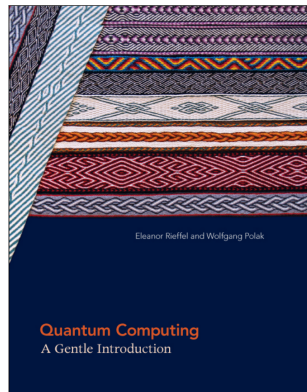
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Topics to be covered (chapter titles)



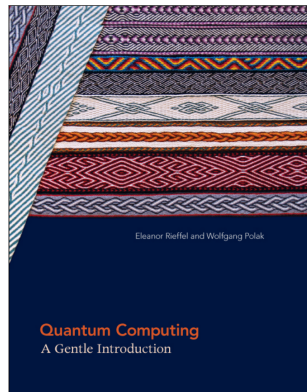
1. Quantum building blocks



Topics to be covered (chapter titles)



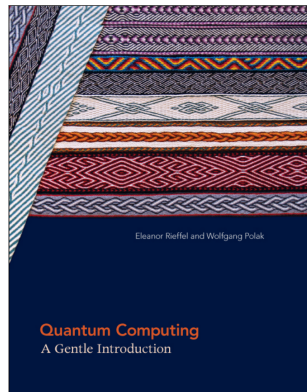
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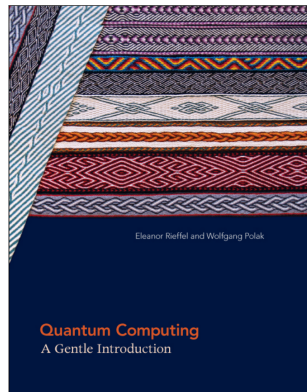
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2. Quantum algorithms
3. Entangled subsystems and robust computation



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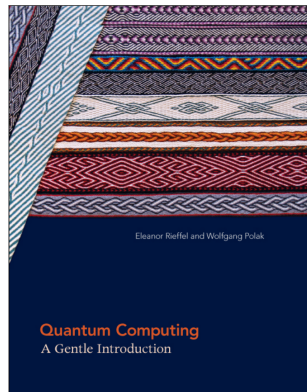
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2. Quantum algorithms
3. Entangled subsystems and robust computation
4. Quantum computing hardware



Topics to be covered (chapter titles)



1. Quantum building blocks
2. Quantum algorithms
3. Entangled subsystems and robust computation
4. Quantum computing hardware
5. Other topics as appropriate



Why study quantum computing?



Quantum computing is one part of a broader field called quantum information science which has revolutionized cryptography and secure communications

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Quantum computing is becoming interesting to a number of fields outside physics and could be even more relevant in the near future

Today's outline - January 13, 2026



Today's outline - January 13, 2026



- Quantum fundamentals

Today's outline - January 13, 2026



- Quantum fundamentals
- Superposition

Today's outline - January 13, 2026



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- Dirac notation

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Reading Assignment: **Reiffel:** 2.4-2.5; 3.1 **Wong:** 2.2.2-2.4.3; 4.2.1-4.2.2

Today's outline - January 13, 2026



- Quantum fundamentals
- Superposition
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Homework Assignment #01:
due Thursday, January 22, 2026

Today's outline - January 13, 2026



- Quantum fundamentals
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Reading Assignment: Reiffel: 2.4-2.5; 3.1 Wong: 2.2.2-2.4.3; 4.2.1-4.2.2

Homework Assignment #01:
due Thursday, January 22, 2026

Homework Assignment #02:
due Tuesday, February 03, 2026

Quantum mechanics fundamentals



A quantum computer is built of qubits which consist of physical systems which have two measureable states

Quantum mechanics fundamentals



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A simple example of such a system is the polarization of a photon

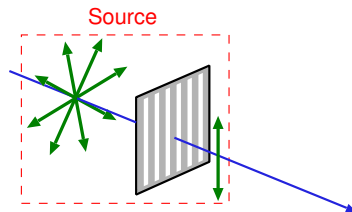
Quantum mechanics fundamentals



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Consider an unpolarized beam of light from a laser pointer prepared in the vertical polarization by a filter



Quantum mechanics fundamentals

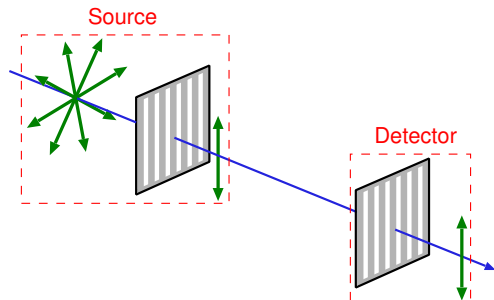


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A detector for the vertical state will detect the full beam intensity,



Quantum mechanics fundamentals

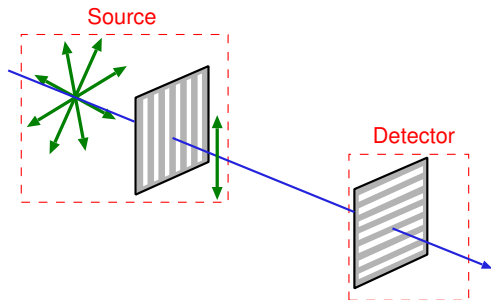


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Consider an unpolarized beam of light from a laser pointer prepared in the vertical polarization by a filter

A detector for the vertical state will detect the full beam intensity, A detector for the horizontal state will detect nothing



Quantum mechanics fundamentals



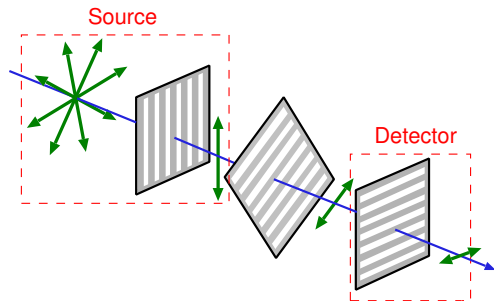
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If a tilted polarizer is placed in between, the horizontal detector now measures a smaller, but non-zero, value



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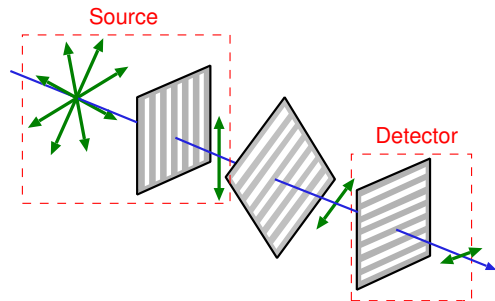
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Because photons are quantum particles, this effect works even for single photons with the measuring a fraction of the photons to be horizontal





Superposition of states

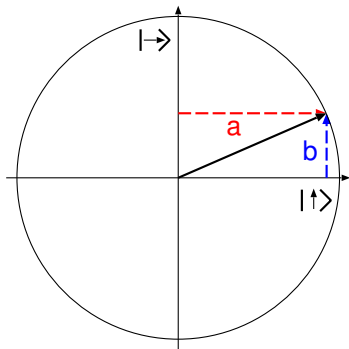
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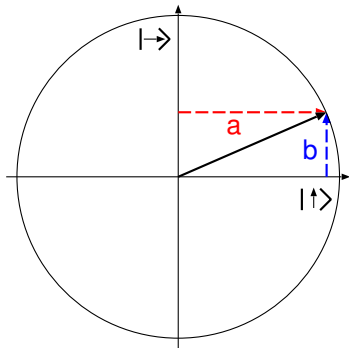
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The state of a single photon can be represented by a generalized quantum superposition of the $|\uparrow\rangle$ and $|\rightarrow\rangle$ states

The amplitudes a and b are complex constants such that the state is normalized

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$$|v|^2 \equiv 1$$





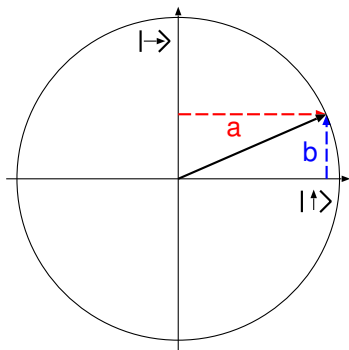
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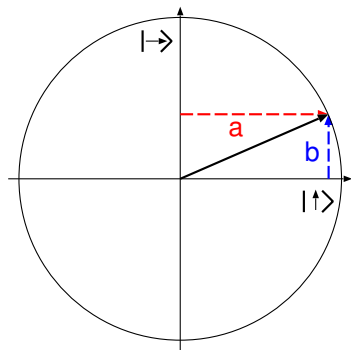




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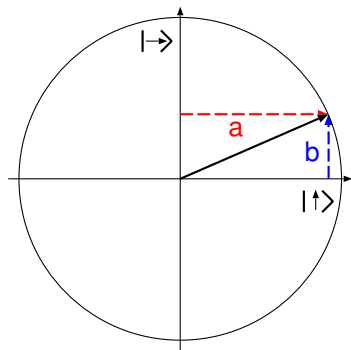
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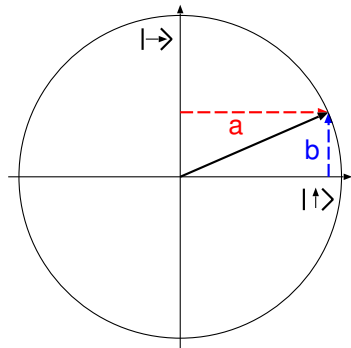
Suppose a photon in a general state $|v\rangle$ enters a detector whose direction is $|\uparrow\rangle$

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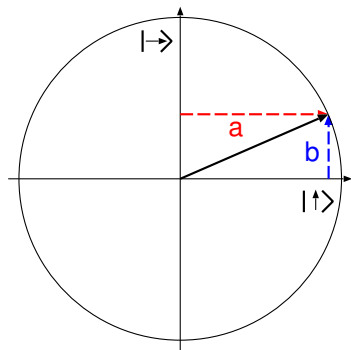
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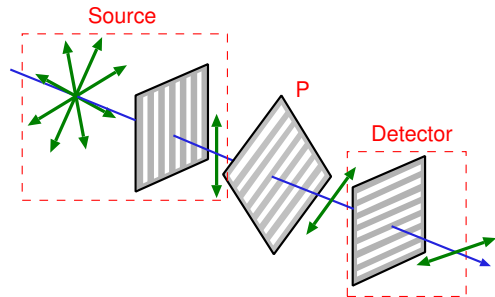
The probability of detection is $|a|^2$ and the probability of absorption is $|b|^2$

This formalism allows us to describe the polarization experiment

Polarizer experiment



The photons that come from the source are in a state $|\uparrow\rangle$

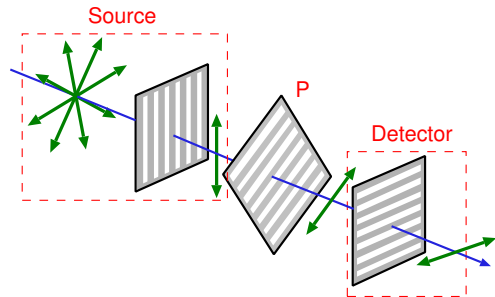


Polarizer experiment



The photons that come from the source are in a state $|\uparrow\rangle$

In the axes of the polarizer P there are two possible states $|\nearrow\rangle$ and $|\nwarrow\rangle$ and the vertically polarized photon can be written as



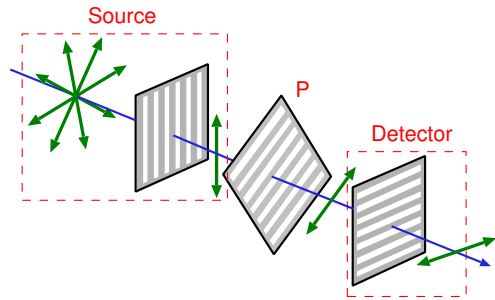
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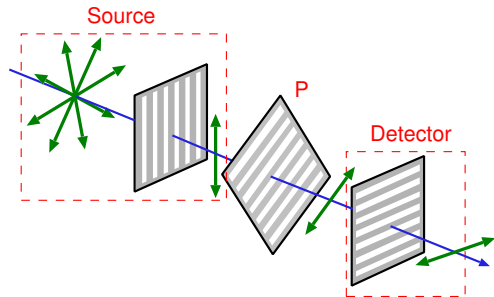


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The photon thus has an 0.5 probability of passing through the polarizer and will then be in a state



Polarizer experiment



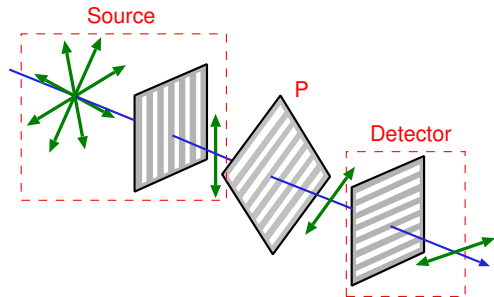
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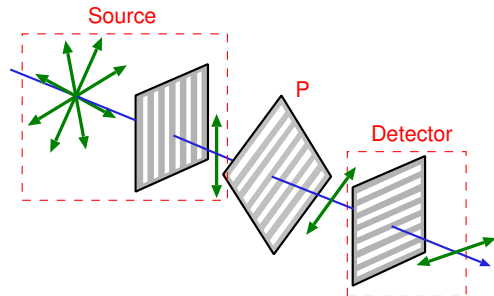
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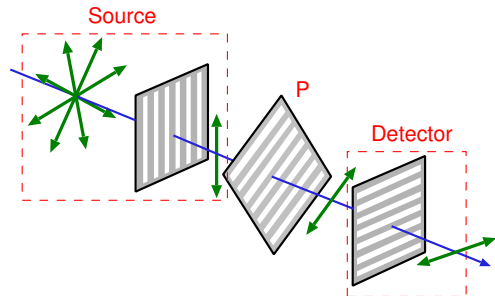
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Quantum particles (and qubits) behave probabilistically





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Examples include photon polarization, electron spin, and ground/excited states of atoms



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A complex vector space V is generated by a set of vectors, S , if every $|v\rangle \in V$ can be written as a complex linear superposition of the vectors in the set



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Dirac, or bra-ket, notation is used to describe quantum systems. The ket ($|x\rangle$) and bra ($\langle x|$) are used to represent a vector and its conjugate transpose respectively

A complex vector space V is generated by a set of vectors, S , if every $|v\rangle \in V$ can be written as a complex linear superposition of the vectors in the set

$$|v\rangle = a_1|s_1\rangle + a_2|s_2\rangle + \cdots + a_n|s_n\rangle,$$



Any two-state quantum system can be considered a qubit and can be modeled as a superposition of the two linearly independent states

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After the measurement any photon that passed through the polarizer is now in the $|\uparrow\rangle$ state

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Realizing an actual quantum computer requires a deep knowledge of quantum mechanics and experimental quantum systems